

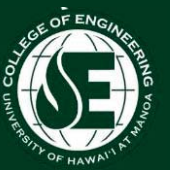
Numerical Analysis of Geosynthetic-Reinforced Soil (GRS) Piers Using Subloading t_{ij} Model

Subloading t_{ij} モデルを用いたジオシンセティック補強土 (GRS) 橋脚の数値解析

Miles Alexander Drazkowski, Phillip S.K. Ooi and Teruo Nakai

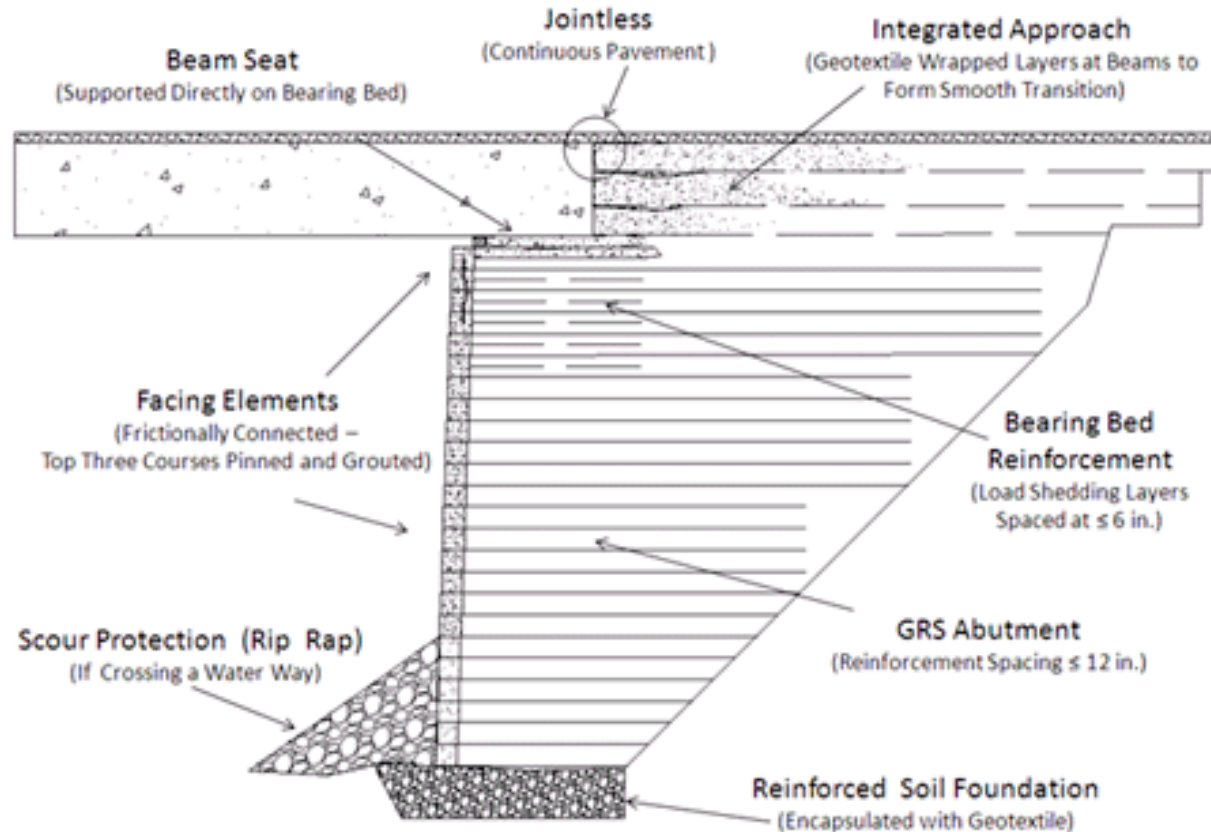
マイルズ ドラズコウスキー, フィリップ S.K. ウーイ, 中井 照夫

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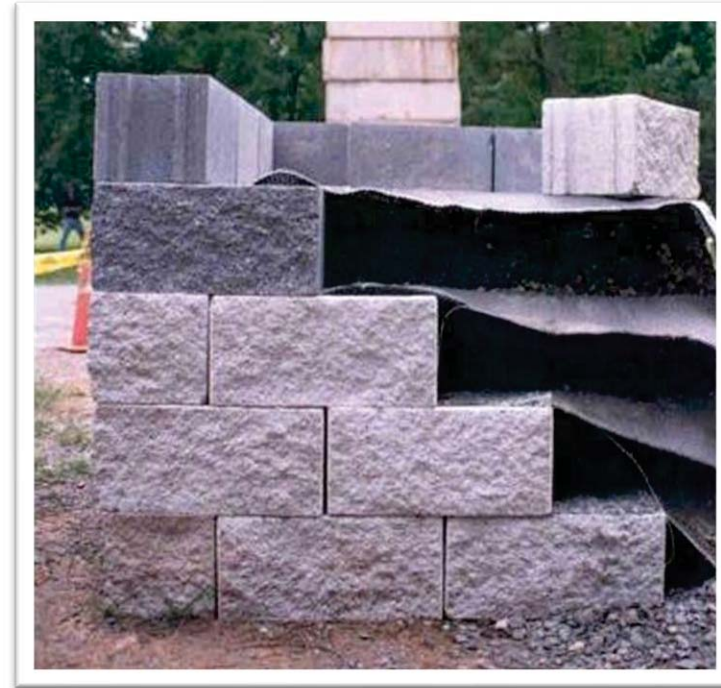


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Introduction はじめに



(Adams et al., 2011)



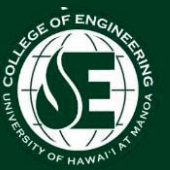
Geosynthetic Reinforced Soil

- Alternating layers of closely spaced (< 30 cm) geosynthetic reinforcement and compacted granular fill

- Fast/cost-effective – eliminate CIP RC abutment walls/footings – superstructure can be precast
- Reduced carbon footprint – manufacture of 1 ton of cement produces 1 ton CO₂
- Can be built in variable weather using common labor, materials and equipment
- **Quality** compaction control – thin lifts between geosynthetics
- High strength capacity- limit states well understood based on numerous large scale load tests

GRS Mini-Piers

GRS橋脚供試体



Faced GRS Mini-Pier (Nicks et. al, 2013)



Unfaced GRS Mini-Pier (Nicks et. al, 2013)

- Large scale load tests of GRS mini-piers conducted at FHWA's Turner-Fairbank Highway Research Center, Mclean, VA
- Faced (CMU) and unfaced mini-piers
- 19 tests using hydraulic jack and load frame
- Various reinforcement spacing, geotextile strength, soil type, faced vs unfaced
- Load, and vertical and lateral deformation monitored

Physical Load Tests

載荷試験



- Cost-prohibitive
- Objective – perform numerical load test

Subloading t_{ij} Model Based on Modified Cam Clay

修正Cam Clayに基づいたSubloading t_{ij} モデル



Modified Cam Clay model (Burland and Roscoe, 1968):

Pros

- First elastoplastic model applicable to practical deformation analysis of soil that
 - Can describe soil behavior during shear and consolidation
 - Can model compressive behavior during strain hardening and dilative behavior during strain softening

Cons

- Does not consider effects of σ_2
- e-log p consolidation curve is bilinear instead of curved
- Data shows trace of Hvorslev's yield surface is not planar in principal stress space, but rather curved
- Cannot model dilation during strain hardening nor strain softening of NC clays
- Cannot handle structured behavior of sensitive clays
- etc.

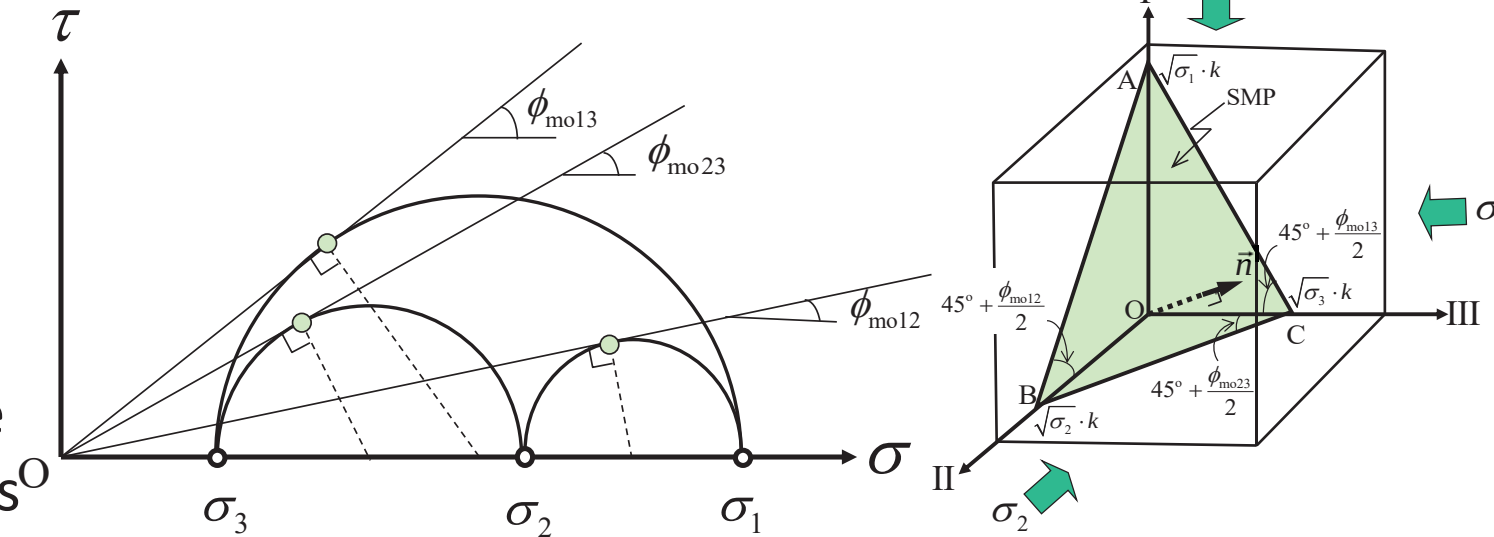
Subloading t_{ij} - Spatially Mobilized Plane

Subloading t_{ij} モデルと空間滑動面 (SMP)

Instead of looking at stresses on octahedral plane, Matsuoka and Nakai (1974) proposed:

- Using stresses on a Spatially Mobilized Plane (SMP)
- SMP coincides with octahedral plane only under isotropic stress conditions (Nakai, 2013).
- SMP is influenced by intermediate principal stress (σ_2)
- SMP is not normal to hydrostatic axis

Matsuoka & Nakai (1974)



$$\tan\left(45^\circ + \frac{\phi_{m o i j}}{2}\right) = \sqrt{\frac{1 + \sin \phi_{m o i j}}{1 - \sin \phi_{m o i j}}} = \sqrt{\frac{\sigma_i}{\sigma_j}} \quad (i, j = 1, 2, 3; i < j)$$

$$I_1 = \sigma_1 + \sigma_2 + \sigma_3$$

$$I_2 = \sigma_1 \sigma_2 + \sigma_2 \sigma_3 + \sigma_3 \sigma_1$$

$$I_3 = \sigma_1 \sigma_2 \sigma_3$$

$$a_1 = \sqrt{\frac{I_3}{I_2 \sigma_1}}, \quad a_2 = \sqrt{\frac{I_3}{I_2 \sigma_2}}, \quad a_3 = \sqrt{\frac{I_3}{I_2 \sigma_3}}$$

Subloading t_{ij} Model

Instead of plotting in principal stress space, Nakai and Mihara (1984) plotted in transformed or t_{ij} stress space

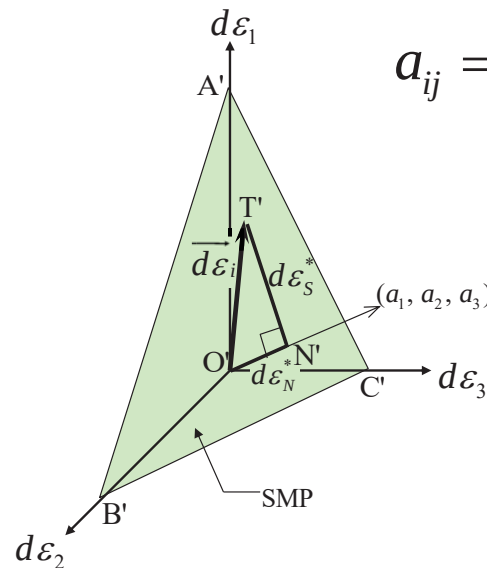
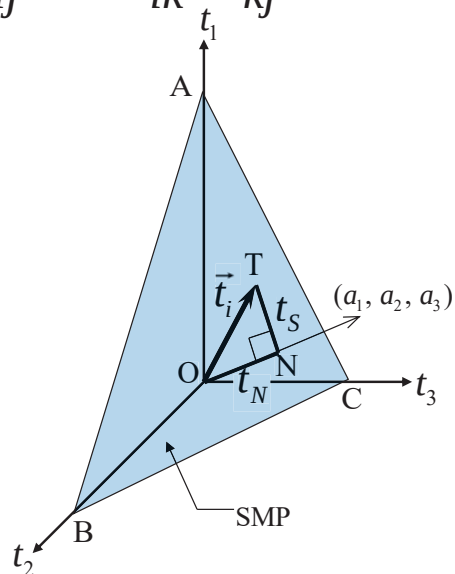
- $t_1 = a_1 \sigma_1$, $t_2 = a_2 \sigma_2$, $t_3 = a_3 \sigma_3$ where, $(a_1, a_2 \text{ and } a_3)$ are direction cosines of normals to SMP

- $t_{ij} = a_{ik} \sigma_{kj}$

$$a_1 = \sqrt{\frac{I_3}{I_2 \sigma_1}}, \quad a_2 = \sqrt{\frac{I_3}{I_2 \sigma_2}}, \quad a_3 = \sqrt{\frac{I_3}{I_2 \sigma_3}}$$

$$a_{ij} = \sqrt{\frac{I_3}{I_2}} \cdot r_{ij}^{-1} = \sqrt{\frac{I_3}{I_2}} \cdot (\sigma_{ik} + I_{r2} \delta_{ik}) (I_{r1} \sigma_{kj} + I_{r3} \delta_{kj})^{-1}$$

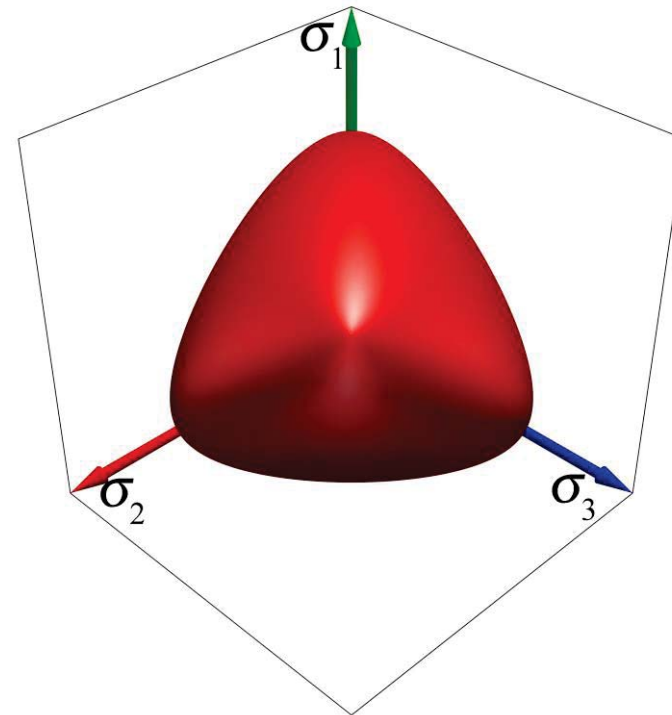
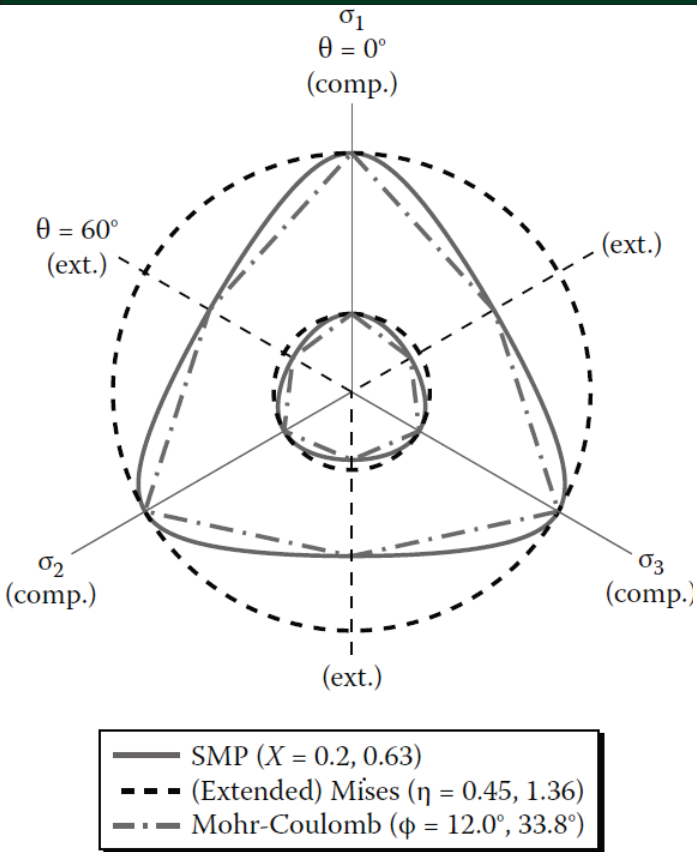
$$(r_{ik} r_{kj} = \sigma_{ij})$$



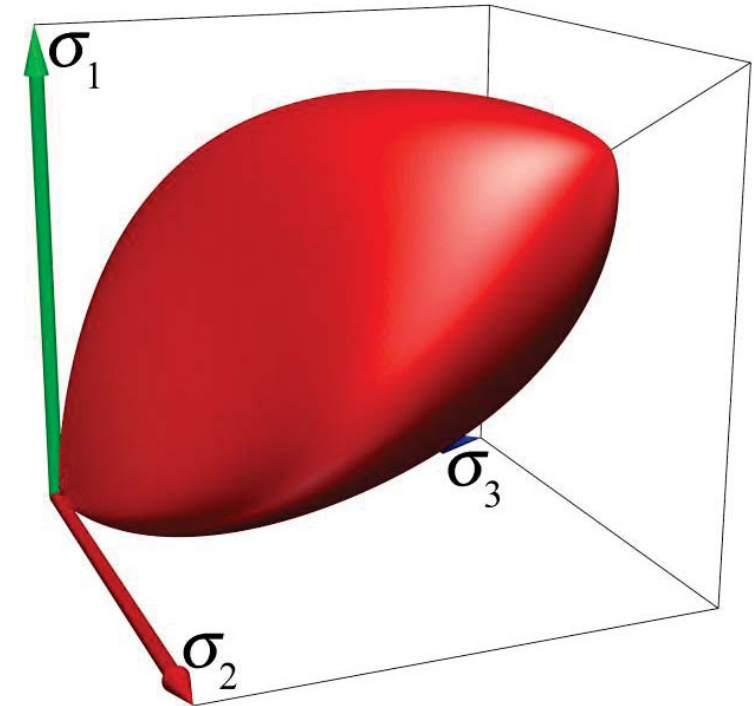
$$\begin{cases} t_N = t_1 a_1 + t_2 a_2 + t_3 a_3 \\ t_S = \sqrt{(t_1 a_2 - t_2 a_1)^2 + (t_2 a_3 - t_3 a_2)^2 + (t_3 a_1 - t_1 a_3)^2} \end{cases}$$

$$\begin{cases} d\epsilon_N^* = d\epsilon_1 a_1 + d\epsilon_2 a_2 + d\epsilon_3 a_3 \\ d\epsilon_S^* = \sqrt{(d\epsilon_1 a_2 - d\epsilon_2 a_1)^2 + (d\epsilon_2 a_3 - d\epsilon_3 a_2)^2 + (d\epsilon_3 a_1 - d\epsilon_1 a_3)^2} \end{cases}$$

Subloading t_{ij} Model



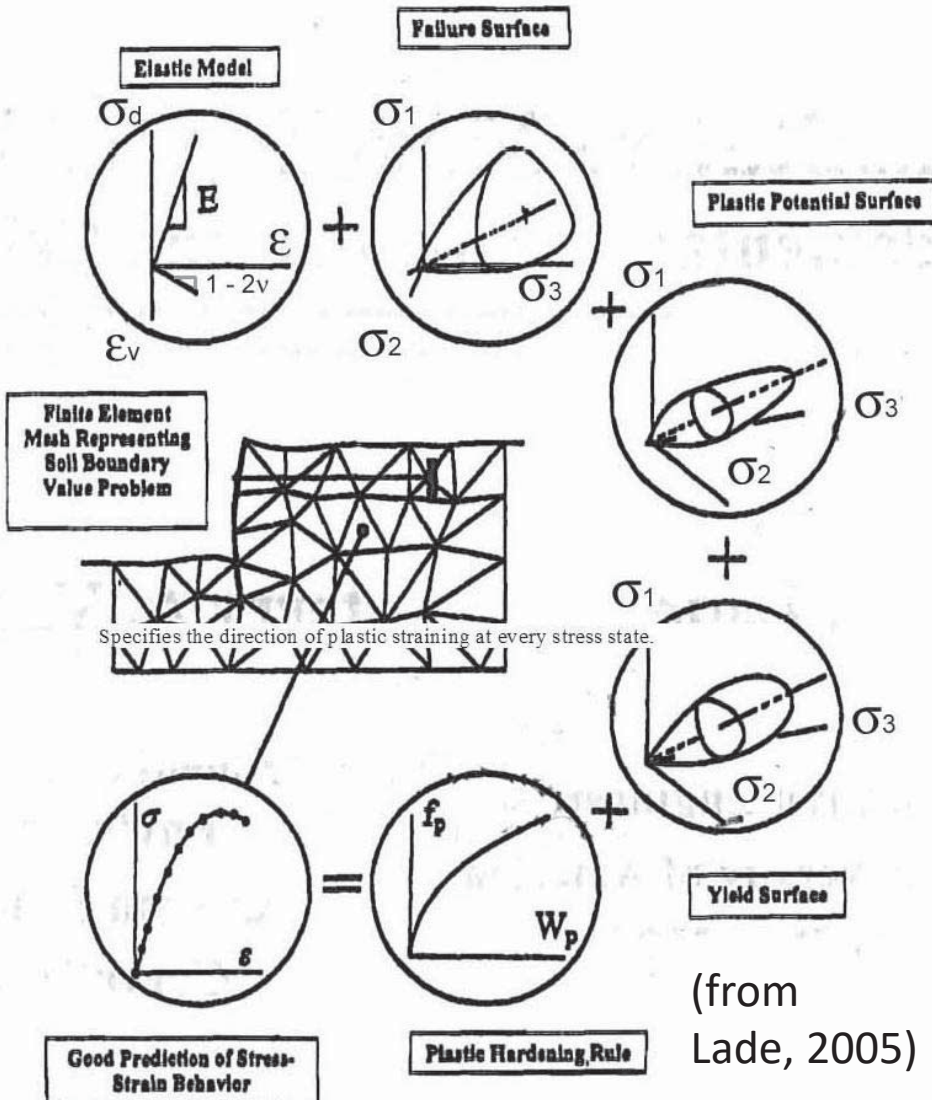
Subloading t_{ij} model is a rounded triangle on hydrostatic axis



Subloading t_{ij} model in σ_1 - σ_2 - σ_3 space

5 Elements of a Elastoplastic Constitutive Model

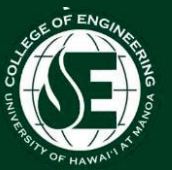
弾塑性モデルを構成する5つの要素



	Component	Function
Elastic Behavior	Hooke's Law	Produces elastic strains whenever the stresses change
Plastic Behavior	Failure Criterion	Imposes limits on stress states that can be reached
	Plastic Potential Function	Produces <u>relative</u> magnitudes of plastic strain increments (similar function as Poisson's ratio for elastic strains)
	Yield Criterion	Determines when plastic strain increments occur: Only when yield surface is pushed out/in (hardening/softening)
	Hardening/Softening Relation	Determines magnitudes of plastic strain increments (similar function as Young's modulus for elastic strains)

Elastic Behavior

彈性挙動



Expression of elastoplastic model:

$$d\varepsilon_{ij} = d\varepsilon_{ij}^e + d\varepsilon_{ij}^p \text{ see later}$$

$$d\varepsilon_{ij}^e = \frac{1+\nu_e}{E_e} d\sigma_{ij} - \frac{\nu_e}{E_e} d\sigma_{mm} \delta_{ij} = C_{ijkl}^e d\sigma_{kl}, \quad E_e = \frac{3(1-2\nu_e)(1+e_0)p}{\kappa}$$
$$\text{or } \left(d\varepsilon_{ij}^e = \frac{1+\nu_e}{E_e} d\left(\frac{\sigma_{ij}}{1+X^2}\right) - \frac{\nu_e}{E_e} d\left(\frac{\sigma_{mm}}{1+X^2}\right) \delta_{ij} = C_{ijkl}^e d\sigma_{kl}, \quad E_e = \frac{3(1-2\nu_e)(1+e_0)t_N}{\kappa} \right)$$

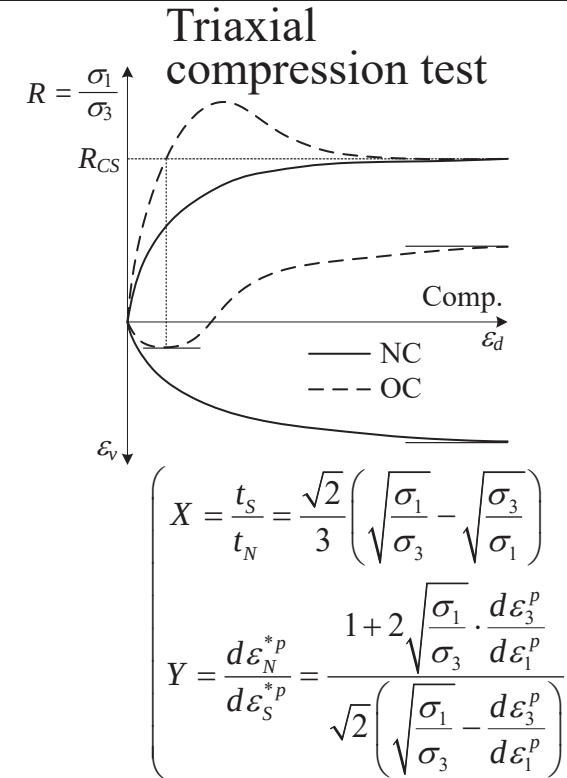
Failure Criterion

破壞基準

Failure criterion based on SMP (Matsuoka & Nakai, 1974)

$$\left\{ \begin{aligned} t_N &= t_1 a_1 + t_2 a_2 + t_3 a_3 \\ &= \sigma_1 a_1^2 + \sigma_2 a_2^2 + \sigma_3 a_3^2 = 3 \frac{I_3}{I_2} = \sigma_{SMP} \\ t_S &= \sqrt{(t_1 a_2 - t_2 a_1)^2 + (t_2 a_3 - t_3 a_2)^2 + (t_3 a_1 - t_1 a_3)^2} \\ &= \sqrt{(\sigma_1 - \sigma_2)^2 a_1^2 a_2^2 + (\sigma_2 - \sigma_3)^2 a_2^2 a_3^2 + (\sigma_3 - \sigma_1)^2 a_3^2 a_1^2} \\ &= \frac{\sqrt{I_1 I_2 I_3 - 9 I_3^2}}{I_2} = \tau_{SMP} \end{aligned} \right.$$

$$\boxed{X = \frac{t_S}{t_N} = \frac{\tau_{SMP}}{\sigma_{SMP}} = \text{const.}} \quad \text{or} \quad \frac{I_3}{I_1 I_2} = \text{const.}$$



at critical state

$$\left\{ \begin{aligned} \boxed{X_{CS} = \frac{\sqrt{2}}{3} \left(\sqrt{R_{CS}} - \frac{1}{\sqrt{R_{CS}}} \right)} \\ Y_{CS} = \frac{1 - \sqrt{R_{CS}}}{\sqrt{2} (\sqrt{R_{CS}} + 0.5)} \end{aligned} \right.$$

Associated Plasticity: Yield Function = Plastic Potential Function

関連流動則：降伏関数＝塑性ポテンシャル関数

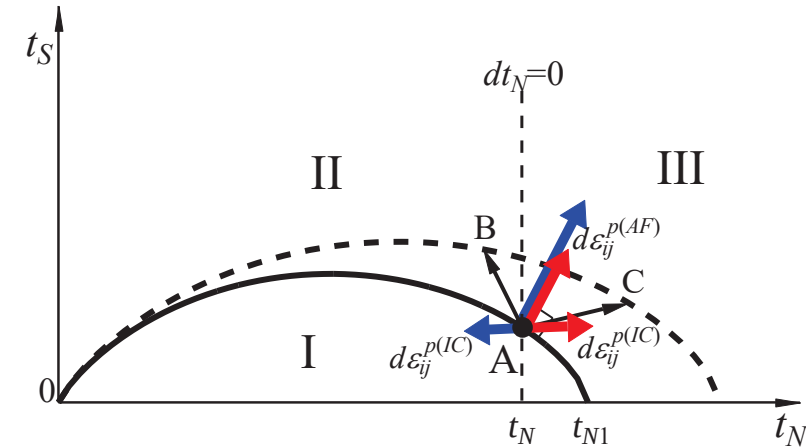
$$\bullet \quad f = F - H - \frac{1}{\lambda - \kappa} (\rho_0 - \rho) = 0$$

$$\bullet \quad d\varepsilon_{ij}^p = \Lambda \frac{\partial F}{\partial t_{ij}} - L^{(IC)} \frac{dt_N}{t_N} \cdot \frac{\frac{\partial F}{\partial t_{ij}}}{\frac{\partial F}{\partial t_{kk}}} + L^{(IC)} \frac{dt_N}{t_N} \cdot \frac{\delta_{ij}}{3} = \left\{ \frac{dF}{h^p} - L^{(IC)} \frac{dt_N}{t_N} \frac{\frac{\partial F}{\partial t_{kk}}}{\frac{\partial F}{\partial t_{kk}}} \right\} \frac{\partial F}{\partial t_{ij}} + L^{(IC)} \frac{dt_N}{t_N} \cdot \frac{\delta_{ij}}{3}$$

$$F = \ln \frac{t_{N1}}{t_{N0}} = \ln \frac{t_N}{t_{N0}} + \varsigma(X), \quad \varsigma(X) = \frac{1}{\beta} \left(\frac{X}{M^*} \right)^\beta$$

(where $X = t_s / t_N$)

$$H = \frac{(-\Delta e)^p}{\lambda - \kappa} = \frac{1 + e_0}{\lambda - \kappa} \varepsilon_v^p$$



Flow rule considering two components
(associated flow and isotropic compression)
of plastic strain increment

$$\left(\begin{aligned} &\text{where, } d\varepsilon_v^p = d\varepsilon_{nn}^p = \Lambda \frac{\partial F}{\partial t_{nn}}, \quad L^{(IC)} = \frac{R^{(IC)}}{h^{p(IC)}} = \frac{\left\langle \frac{\partial F}{\partial t_{kk}} \frac{t_N}{\sqrt{3}} \right\rangle^2}{h^{p(IC)}} \\ &h^p = \frac{1 + e_0}{\lambda - \kappa} \left\{ \frac{\partial F}{\partial t_{kk}} + \sqrt{3} \frac{G/(1 + k_a X) + Q/(1 + k_b X)}{t_N} \right\}, \quad h^{p(IC)} = \frac{1 + e_0}{\lambda - \kappa} \left\{ 1 + \left\langle G/(1 + k_a X) + Q/(1 + k_b X) \right\rangle \right\} \end{aligned} \right) \text{ for both bonding and density effects}$$

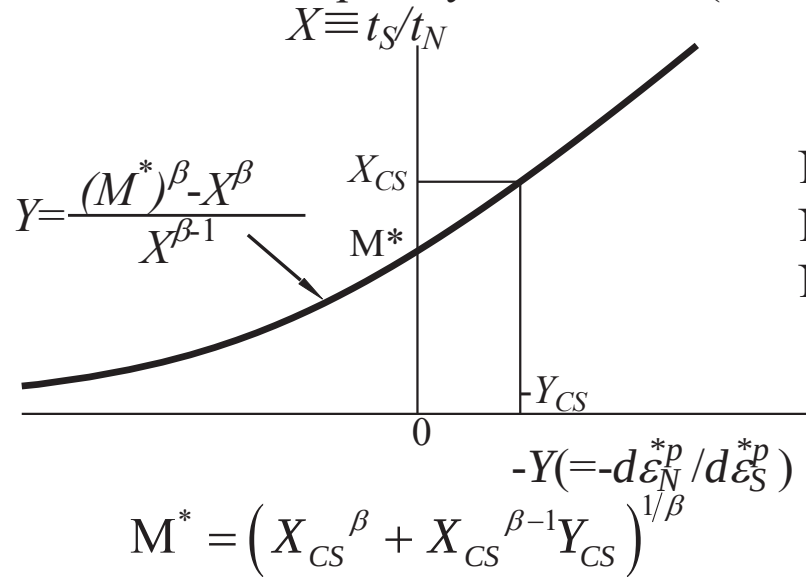
Loading $\left(\begin{aligned} &d\varepsilon_{ij}^p = d\varepsilon_{ij}^{p(AF)} + d\varepsilon_{ij}^{p(IC)} \neq 0 \quad \text{if } \Lambda = \frac{dF}{h^p} \geq 0 \\ &d\varepsilon_{ij}^p = 0 \quad \text{otherwise} \end{aligned} \right.$

Nakai (2022)

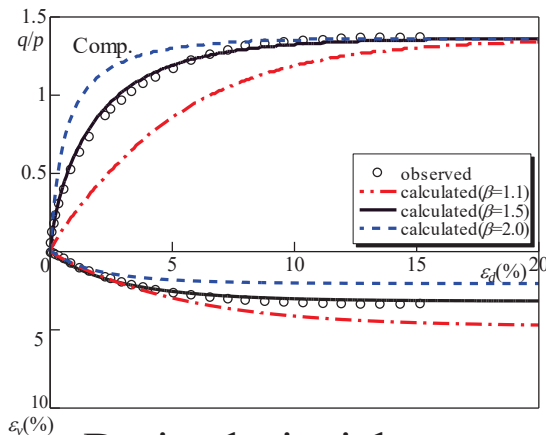
Formulation of model based on t_{ij} concept

t_{ij} の概念に基づくモデルの定式化

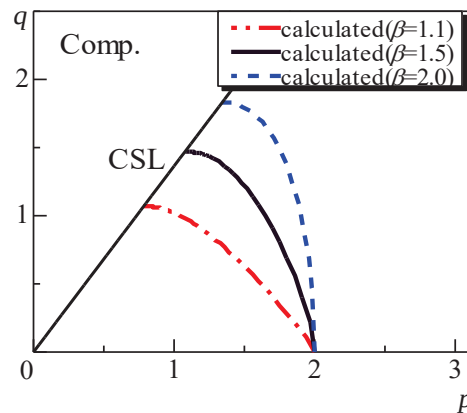
- Method to determine the shape of yield surface (stress-dilatancy relation)



Nakai and Matsuoka (1986)
Nakai and Hinokio (2004)
Nakai (2013)

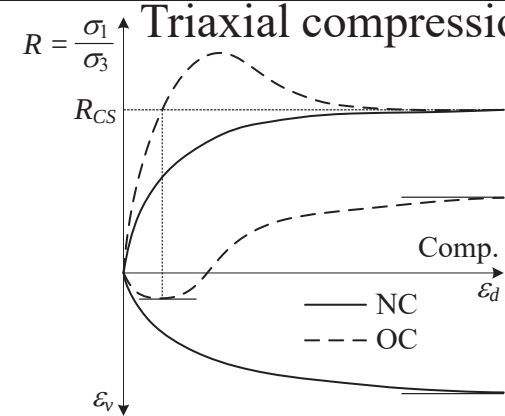


Drained triaxial test



Undrained triaxial test

Triaxial compression test



$$\begin{cases} X = \frac{t_S}{t_N} = \frac{\sqrt{2}}{3} \left(\sqrt{\frac{\sigma_1}{\sigma_3}} - \sqrt{\frac{\sigma_3}{\sigma_1}} \right) \\ Y = \frac{d\varepsilon_N^p}{d\varepsilon_S^p} = \frac{1 + 2\sqrt{\frac{\sigma_1}{\sigma_3}} \cdot \frac{d\varepsilon_3^p}{d\varepsilon_1^p}}{\sqrt{2} \left(\sqrt{\frac{\sigma_1}{\sigma_3}} - \frac{d\varepsilon_3^p}{d\varepsilon_1^p} \right)} \end{cases}$$



At critical state

$$\begin{cases} X_{CS} = \frac{\sqrt{2}}{3} \left(\sqrt{R_{CS}} - \frac{1}{\sqrt{R_{CS}}} \right) \\ Y_{CS} = \frac{1 - \sqrt{R_{CS}}}{\sqrt{2} (\sqrt{R_{CS}} + 0.5)} \end{cases}$$

Hardening Relation

硬化則



$$\Lambda = \frac{dF}{\frac{1+e_0}{\lambda-\kappa} \left\{ \frac{\partial F}{\partial t_{kk}} + \sqrt{3} \frac{\frac{G}{(1+k_a X)} + \frac{Q}{(1+k_b X)}}{t_N} \right\}} = \frac{dF}{h^p}$$

$$d\varepsilon_{ij}^p = \frac{dF}{h^p} \cdot \frac{\partial F}{\partial t_{ij}} - L^{(IC)} \frac{dt_N}{t_N} \frac{\frac{\partial F}{\partial t_{ij}}}{\frac{\partial F}{\partial t_{kk}}} + L^{(IC)} \frac{dt_N}{t_N} \frac{\delta_{ij}}{3}$$

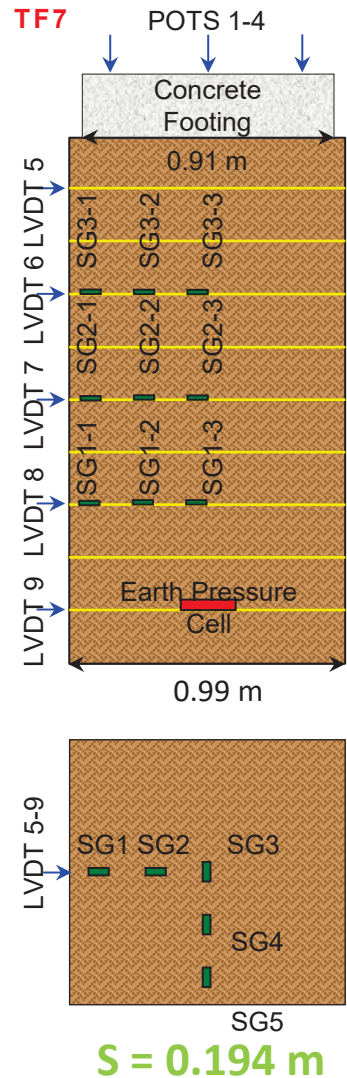
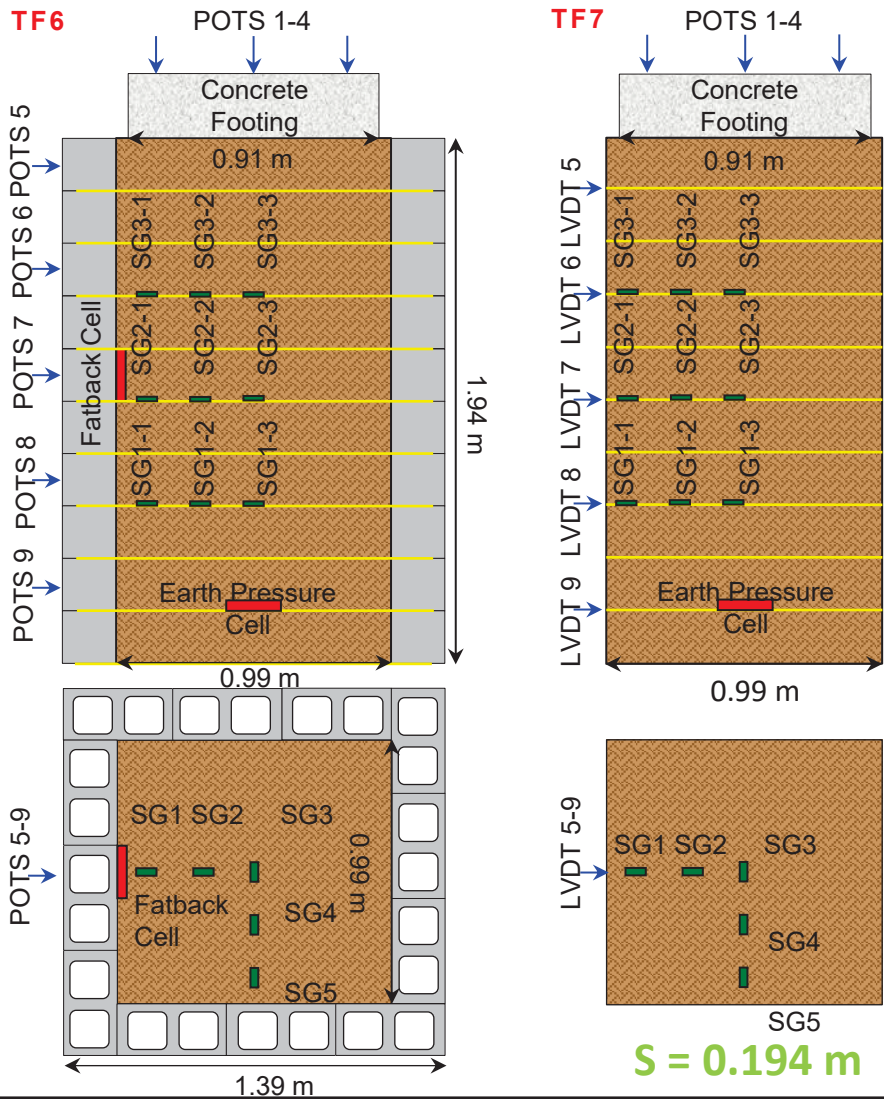
$$\left(\begin{array}{l} \text{where, } h^p = \frac{1+e_0}{\lambda-\kappa} \left\{ \frac{\partial F}{\partial t_{kk}} + \sqrt{3} \frac{\frac{G}{(1+k_a X)} + \frac{Q}{(1+k_b X)}}{t_N} \right\} \\ L^{(IC)} = \frac{R^{(IC)}}{h^{p(IC)}} = \frac{\left| \frac{\partial F}{\partial t_{kk}} \frac{t_N}{\sqrt{3}} \right|^m}{h^{p(IC)}} \text{ (usually } m = 2) \\ h^{p(IC)} = \frac{1+e_0}{\lambda-\kappa} \left\{ 1 + \left| \frac{G}{(1+k_a X)} + \frac{Q}{(1+k_b X)} \right| \right\} \end{array} \right)$$

Loading condition:

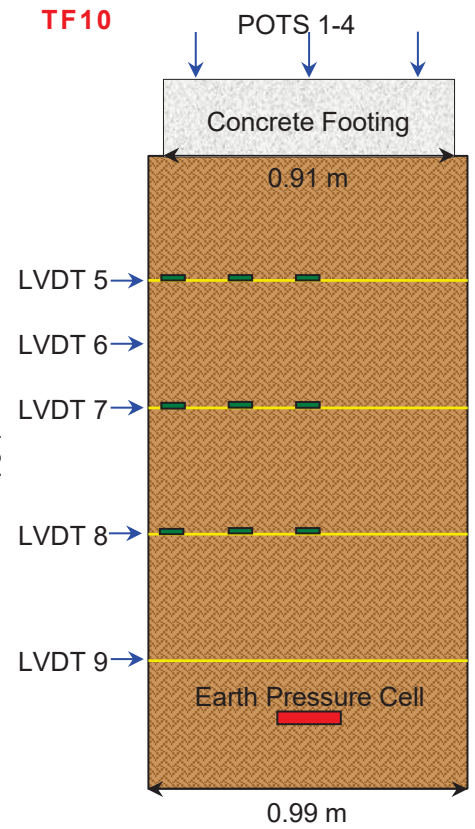
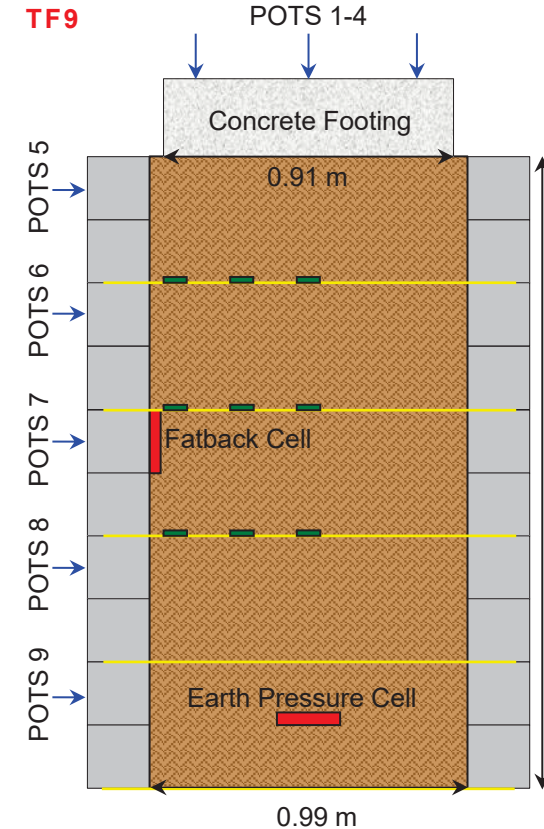
$$\left(\begin{array}{l} d\varepsilon_{ij}^p \neq 0 \text{ if } \Lambda = \frac{dF}{h^p} > 0 \\ d\varepsilon_{ij}^p = 0 \text{ otherwise} \end{array} \right)$$

GRS Column Setup

GRSの設置



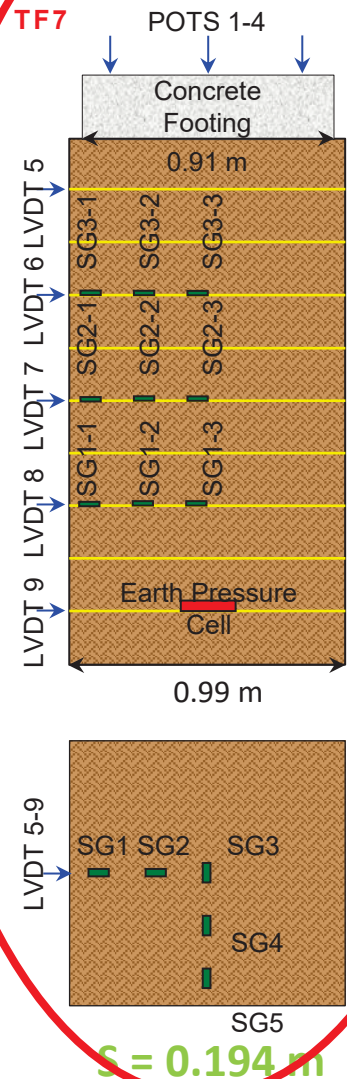
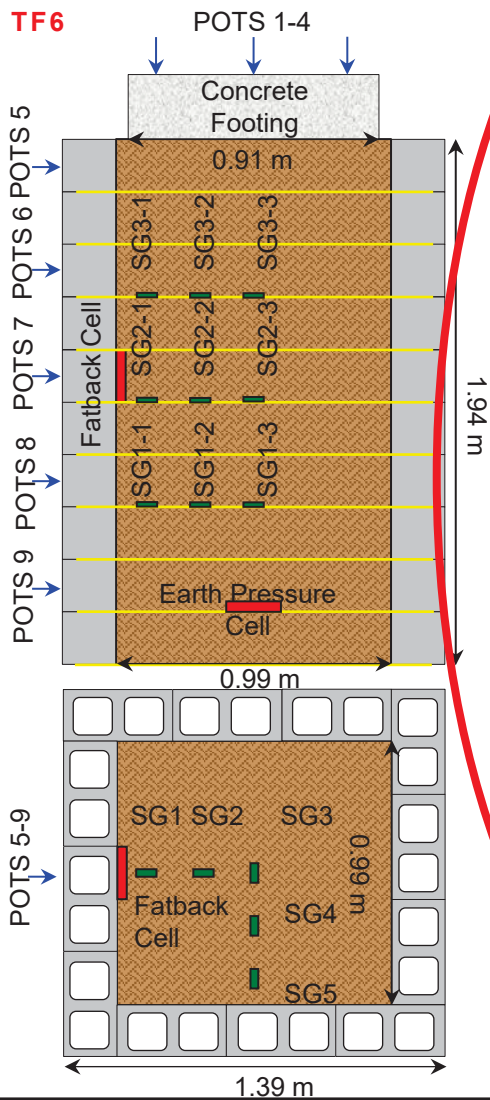
- 0.99 x 0.99 x 1.94 m composite GRS column with alternating layers of granular fill and geosynthetic
- Columns have a 2:1 height-to-width ratio to minimize end effects
- Faced and un-faced columns constructed using same procedure with un-faced having facing removed during final step



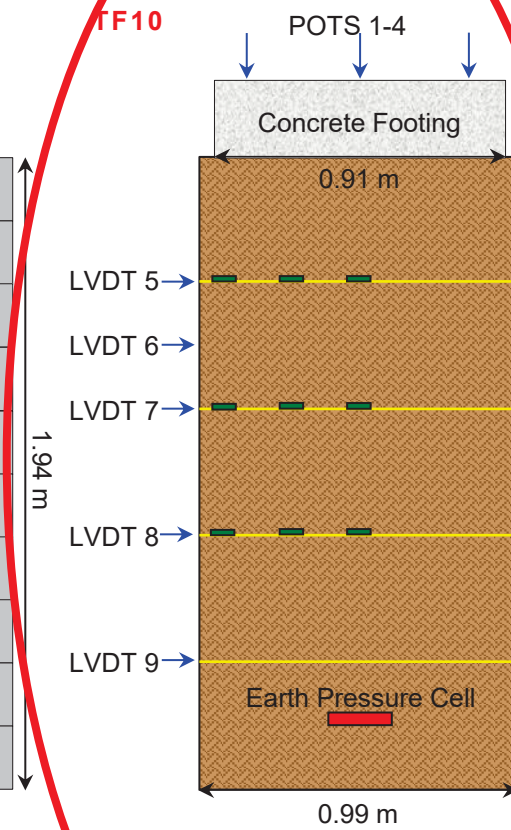
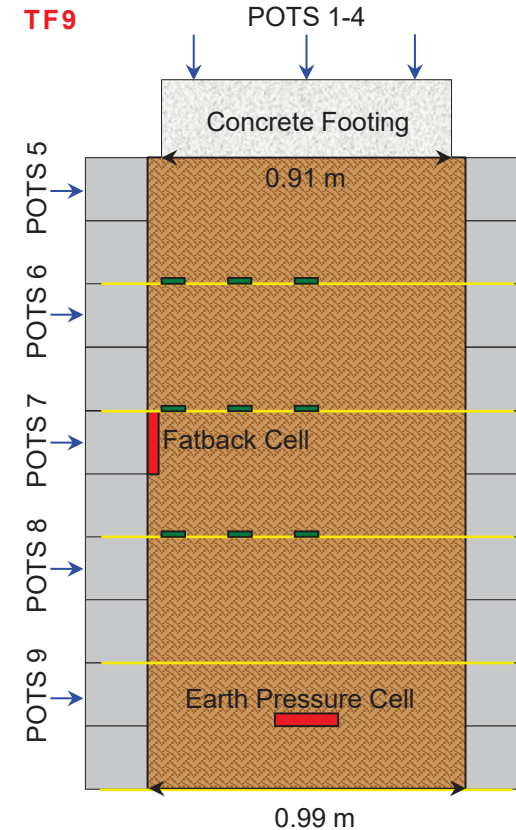
S = 0.389 m

GRS Column Setup

GRSの設置



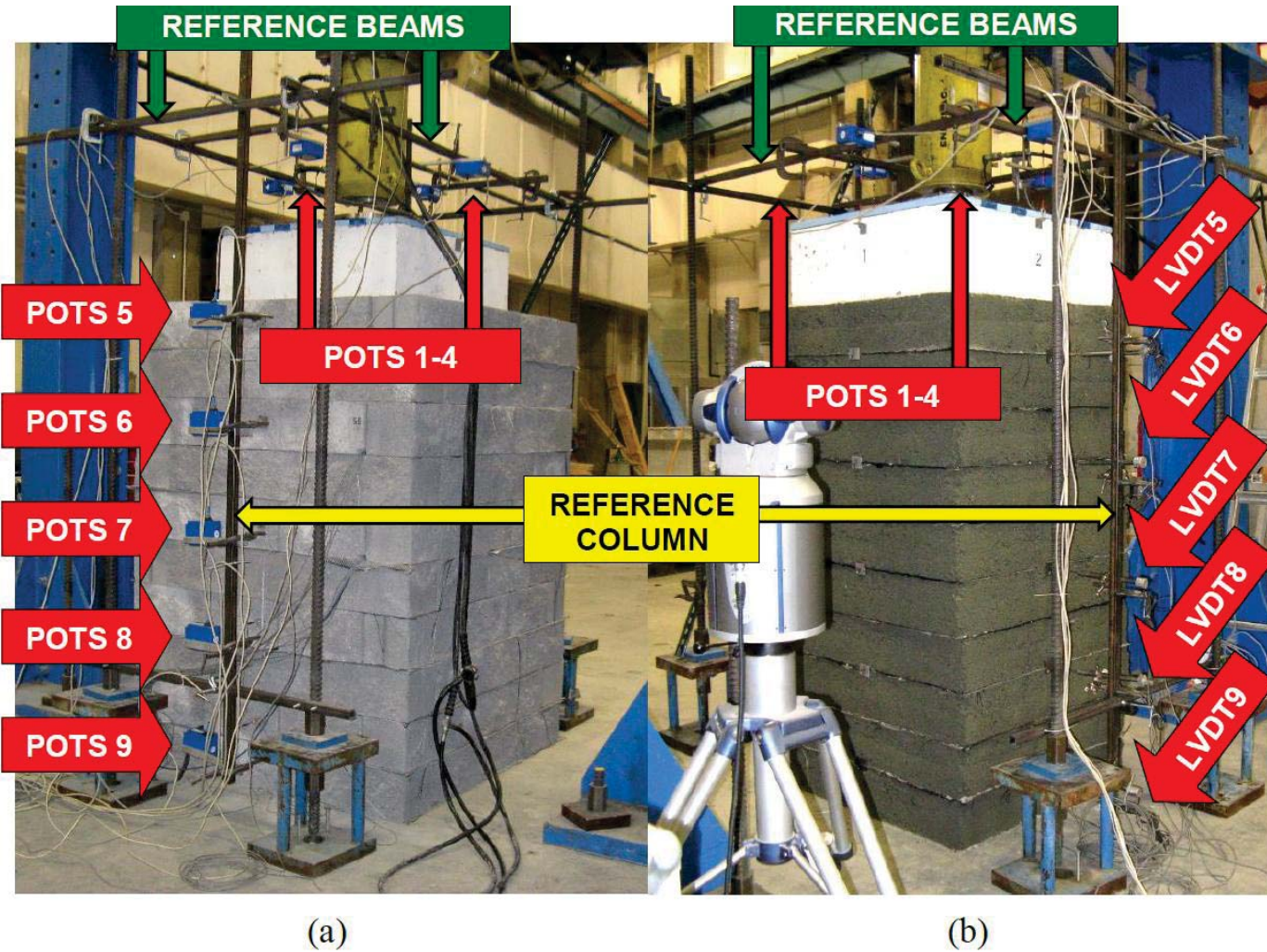
- 0.99 x 0.99 x 1.94 m composite GRS column with alternating layers of granular fill and geosynthetic
- Columns have a 2:1 height-to-width ratio to minimize end effects
- Faced and un-faced columns constructed using same procedure with un-faced having facing removed during final step



$S = 0.389 \text{ m}$

Load Testing

載荷試驗



Schematics of deflection instrumentation for mini piers (a) with facing and (b) without facing. (Iwamoto, 2014)



TF-10 at failure with $S_v = 15\frac{1}{4}$ inches, $T_f = 4,800$ lb/ft, and VDOT 21A material. (Nicks et al., 2013)

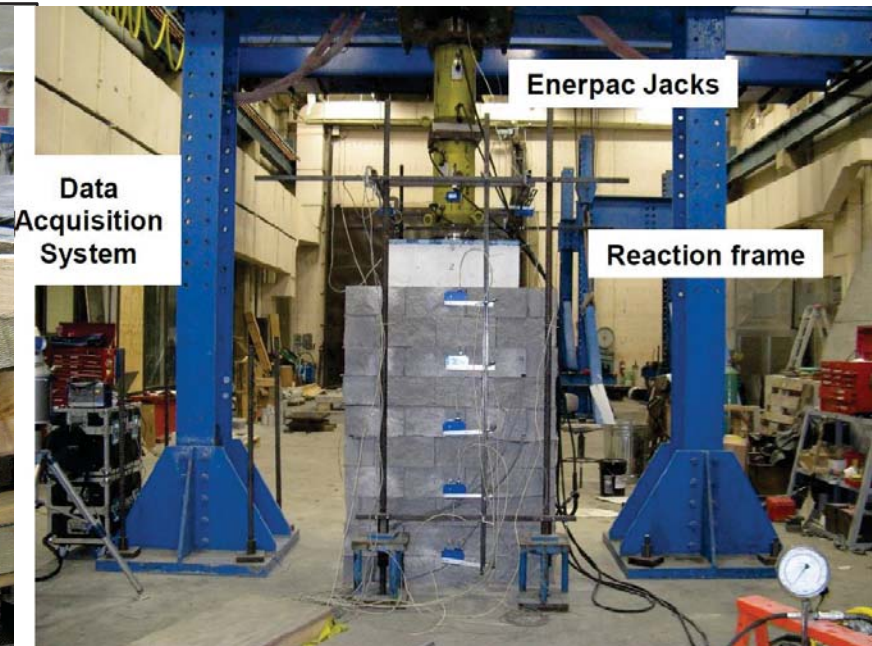
Staged Construction

段階施工



PLATE COMPACTOR

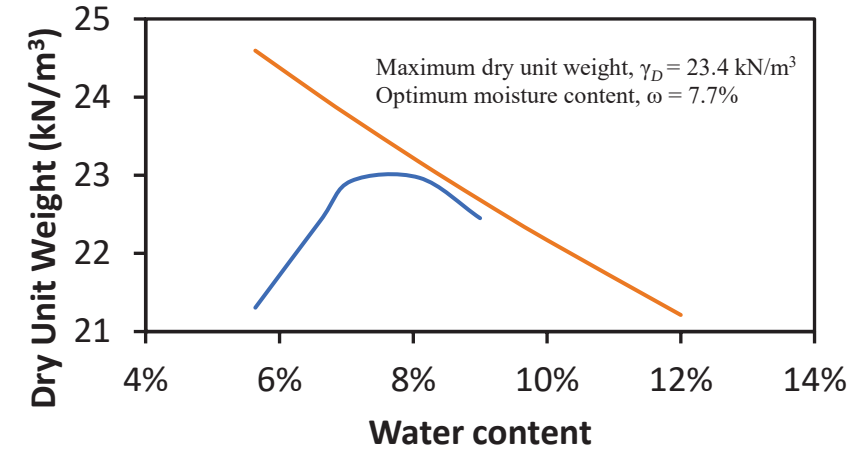
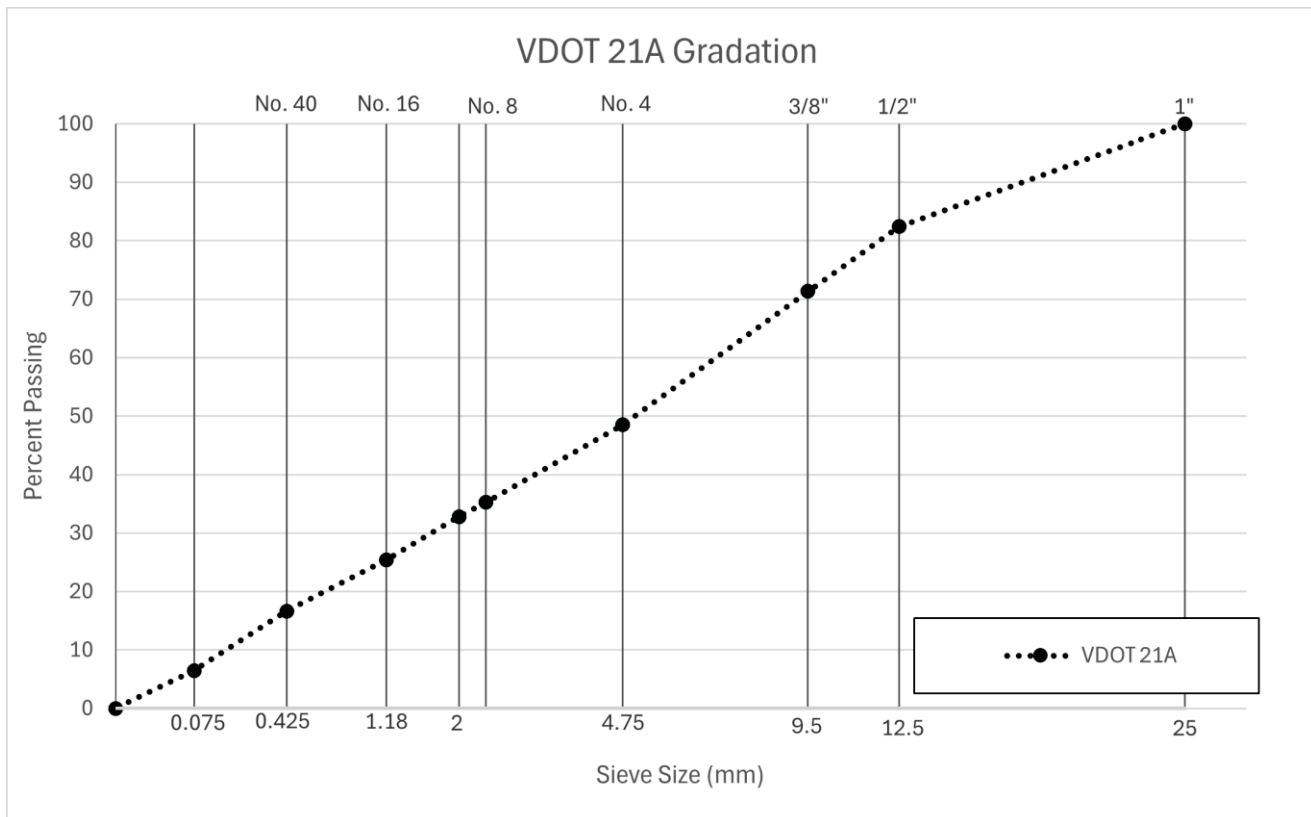
The Patchman PM-1012[®] Plate Compactor with a 10" x 10" plate and a 12 Volt DC Model DC-700 vibrator (115 volt 1 phase units also available) which creates 700 lbs. of adjustable impact force. Ideal for compacting next to foundations, in narrow trenches or other tight spots. Also ideal for D.O.T. or Public Works crews for pothole patching. Easy hook-up to trailer light receptacle, 30' of cord for complete mobility. Comes complete with male and female receptacle. Weight only 48 lbs.



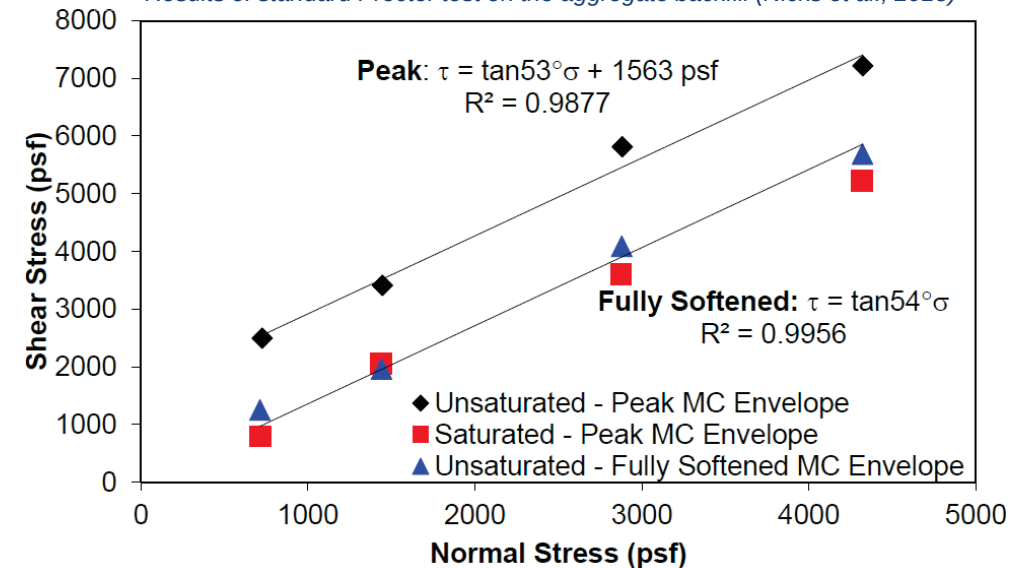
Backfill

埋め戻し

Well-graded gravel with silt (GW-GM) from Lucky Stone quarry in Leesburg, VA used as base course



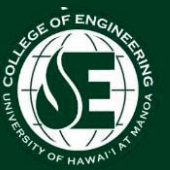
Results of standard Proctor test on the aggregate backfill (Nicks et al., 2013)



Comparison of saturated, unsaturated, and fully softened Mohr-Coulomb envelopes. (Iwamoto, 2014)

Soil Parameters

土質パラメータ



Parameter	Value	
λ	0.0325	Same parameters as modified Cam-clay model
κ	0.0016	
$N = e_{NC}$ at 1 atm	0.364	
$R_{CS} = (\sigma_1/\sigma_3)_{CS\ comp}$	5	
ν_e	0.2	
β	1.155	Shape of yield surface
a	400	Influence of density
k_a	10	
b	0	Influence of bonding
$Q_o = b\omega_o$	0	
k_b	0	
e_{max}	0.55	Max. e since p plotted on log scale



Normally consolidated



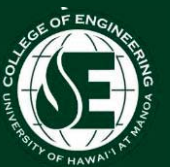
Over consolidated



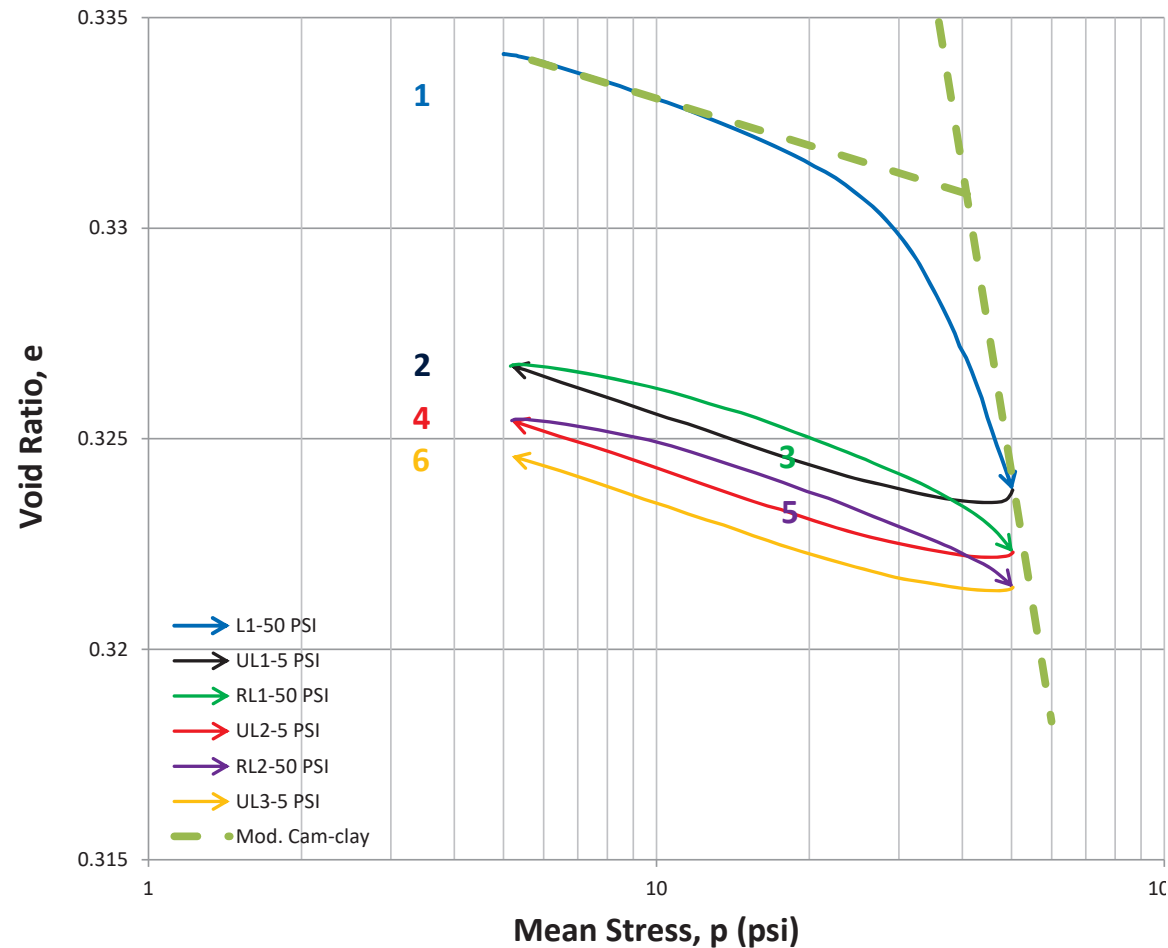
Structured clay

Isotropic Consolidation

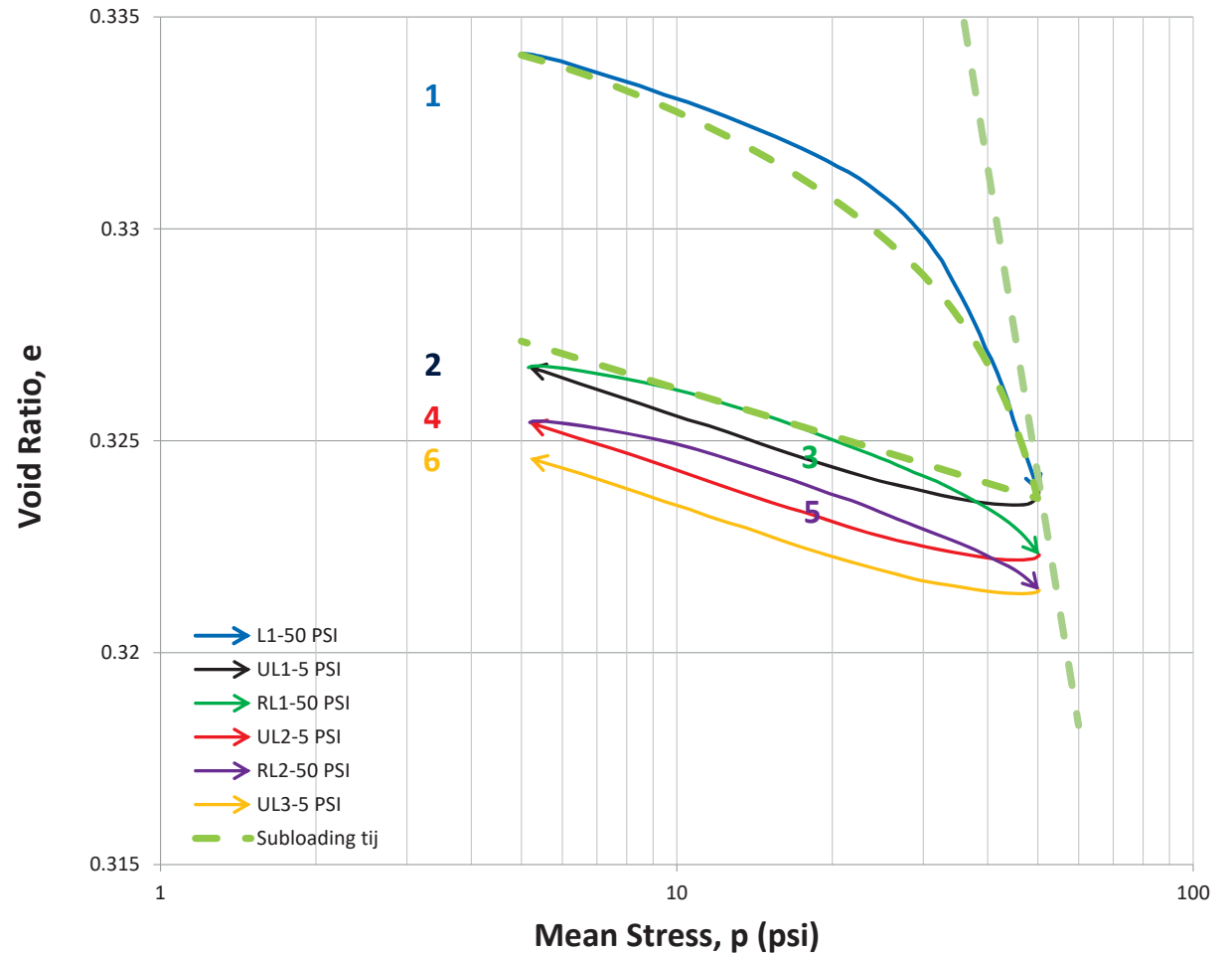
等方圧縮



Modified Cam-clay



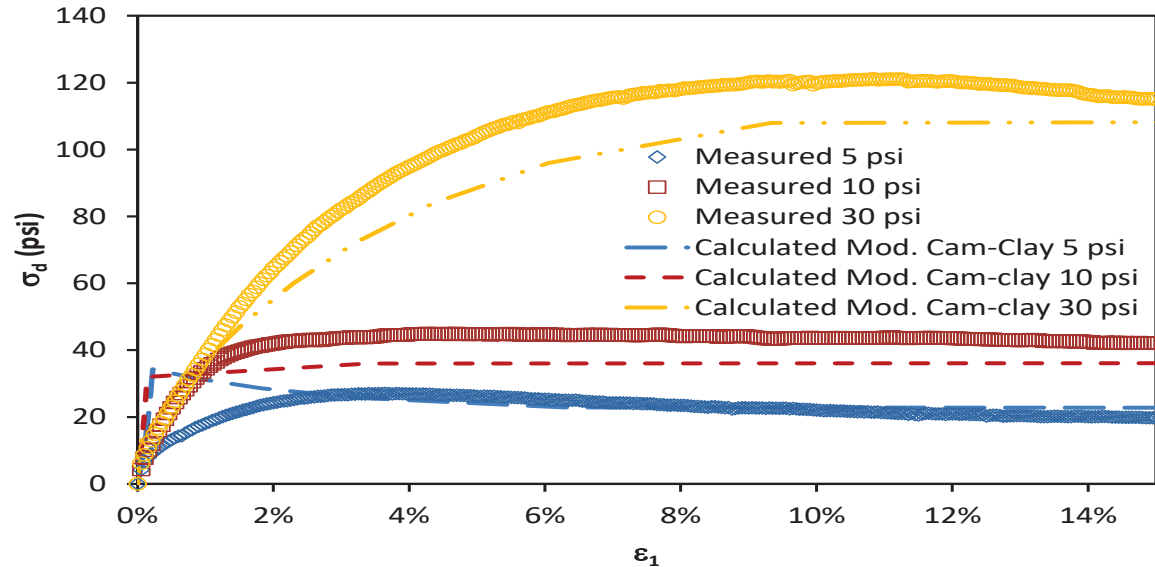
Subloading t_{ij}



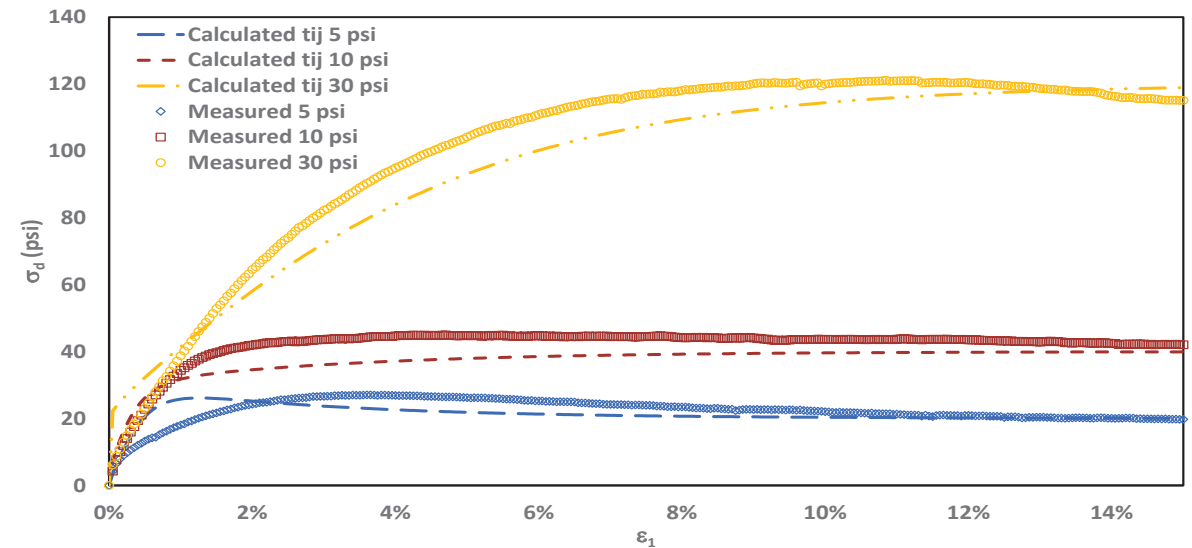
CD Triaxial Test – Model vs Measured

CD三軸試験：モデルによる解析と実測値の比較

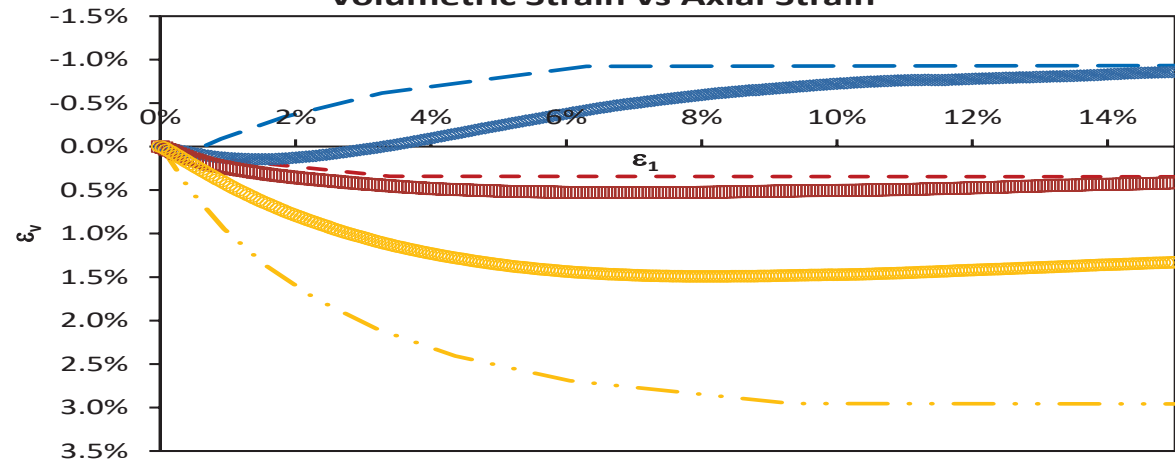
Deviator Stress vs Axial Strain



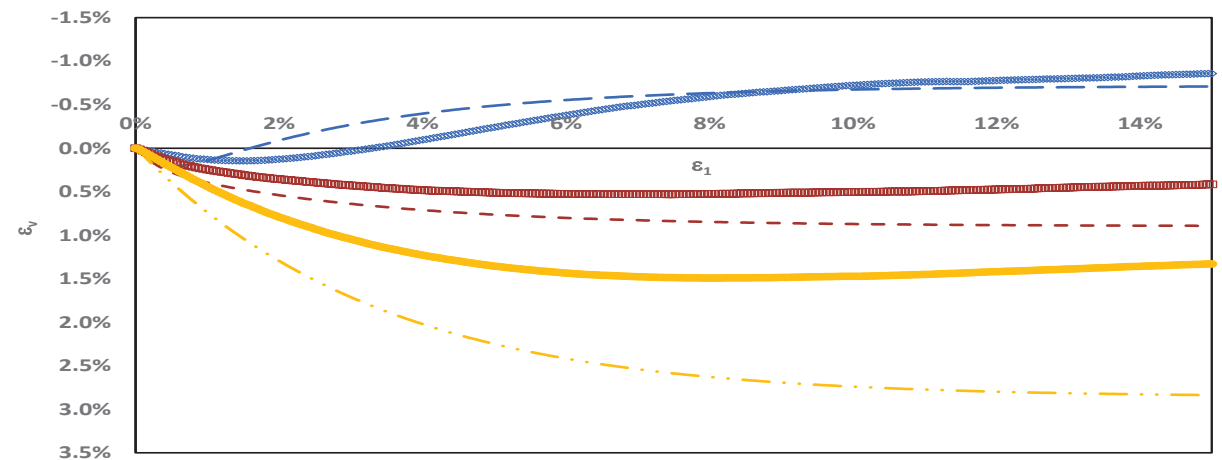
Deviator Stress vs Axial Strain



Volumetric Strain vs Axial Strain



Volumetric Strain vs Axial Strain



Parameter Optimization - ML

パラメータ最適化 - 機械学習



Traditional Methods (in order of Reliability):

- Analytical Derivation
- Literature Values (interface properties)
- Manual Iteration

Subloading tij Parameter Optimization:

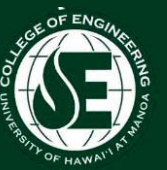
- Subloading tij_a.exe (Para, Path, and Ana.cal files)
- Manual Iteration
- Limitations/Constraints

Potential path forward:

- Machine Learning based optimization
- Inverse Problem (Zhang et al., 2021)
- Genetic Algorithms
 - Pal et al. (1996), Samarajiva et al. (2005), and Rokonuzzaman and Sakai (2010)
- Bayesian Inference
 - Sakai and Nakano (2025), Coelho et al. (2024)

Machine Learning Framework

機械学習モデル構築の枠組み



Bayesian Inference and Maximum-Likelihood approach

$$p(\Theta, \alpha | D) = \frac{1}{Z} p(\Theta, \alpha) p(D | \Theta, \alpha)$$

Θ is the set of model parameters

α is the set of nuisance parameters

D is the set of observations

$p(\Theta, \alpha)$ is the prior distribution

$p(D | \Theta, \alpha)$ is the likelihood function computed for any particular value of (Θ_i, α_i)

$Z = p(D)$ is the normalization and is independent of Θ and α

Machine Learning Framework

機械学習モデル構築の枠組み



Markov chain Monte Carlo (MCMC) optimization for multi-variable optimization problems (Foreman-Mackey et al., 2013):

- Bayesian inference, computing and utilizing the posterior probability density function (PDF) for the model parameters
- Markov Chain - next step (set of sampling locations in the posterior probability) depends on previous set
- Monte Carlo - the approximation of the probability density functions is based on a Monte Carlo approach

Approximate posterior PDF efficiently despite parameter spaces with **high dimensionality**. “emcee” algorithm as its **affine invariance** results in performance independent of highly anisotropic posterior PDFs (Goodman & Weare, 2010)

Basis of emcee algorithm is the **Metropolis-Hastings** (M-H) algorithm with an **affine invariant** process

Compute **N samples (steps)** $\{\Theta_i\}$ from the posterior PDF (Foreman-Mackey et al., 2013)

Machine Learning Framework

機械学習モデル構築の枠組み



- *emcee* algorithm generates a random walk in the parameter space, $X(t_i) = [\Theta_i, \alpha_i]$ depending only on previous step $X(t_{i-1})$.
- Affine-invariance means use of a simultaneously evolving ensemble of K “walkers”, $S = \{X_k\}$.
- Proposed parameter distribution for the k th walker is based on the current positions of the $K - 1$ walkers in ensemble $S[k] = \{X_j, \forall_j \neq k\}$.
- Position of walker X_k is updated by drawing random walker X_j from the ensemble $S[k]$ (Goodman & Weare, 2010).

if $r \leq q$ then

$X_k(t + 1) \leftarrow Y$

else

$X_k(t + 1) \leftarrow X_k(t)$

endif

where r is a random sample from a uniform distribution $r \sim U[0, 1]$

and Y is updated walker position

$$X_k(t) \rightarrow Y = X_j + Z[X_k(t) - X_j]$$

where Z is a random variable drawn from $g(Z = z)$.

$$g(z^{-1}) = zg(z)$$

$$g(z) \propto \begin{cases} \frac{1}{\sqrt{z}} & \text{if } z \in \left[\frac{1}{a}, a\right] \\ 0 & \text{otherwise} \end{cases}$$

where $a > 1$ (often set to 2).

Acceptance probability q :

$$q = \min\left(1, Z^{N-1} \frac{p(Y)}{p(X_k(t))}\right)$$

Parameters from Machine Learning but....

機械学習から得られたパラメータだが...

The magnitude problem and proposed weighting schema:

1. Min-max normalization scheme:

$$\frac{1}{w_i} = 0.01 + \frac{x_i - \min(x)}{\max(x) - \min(x)}$$

2. Logarithmic weighing scheme:

$$w_i = \begin{cases} \frac{1}{\log x_i} & \text{for } x_i \geq 1 \\ \frac{1}{|\log(1000 * x_i)|} & \text{for } x_i \leq 1 \end{cases}$$

3. Reverse Sequential weighing scheme:

$$w_i = \frac{i}{\text{count}(x)} * (\max(x) - \min(x))$$

Parameters from Machine Learning

機械学習によるパラメータ

Parameter	Value	Description
N	0.3576	Void ratio at reference pressure (1 atm)
λ	0.0207	Virgin compression index (slope of NC line)
β	1.0515	Yield function shape parameter
a	103.32	Density function parameter
k_a	1.0	Shear control parameter for density function
R_{cs}	5.0852	Principal stress ratio at critical state in triaxial compression

Additional Outputs:

χ^2

Reduced χ^2

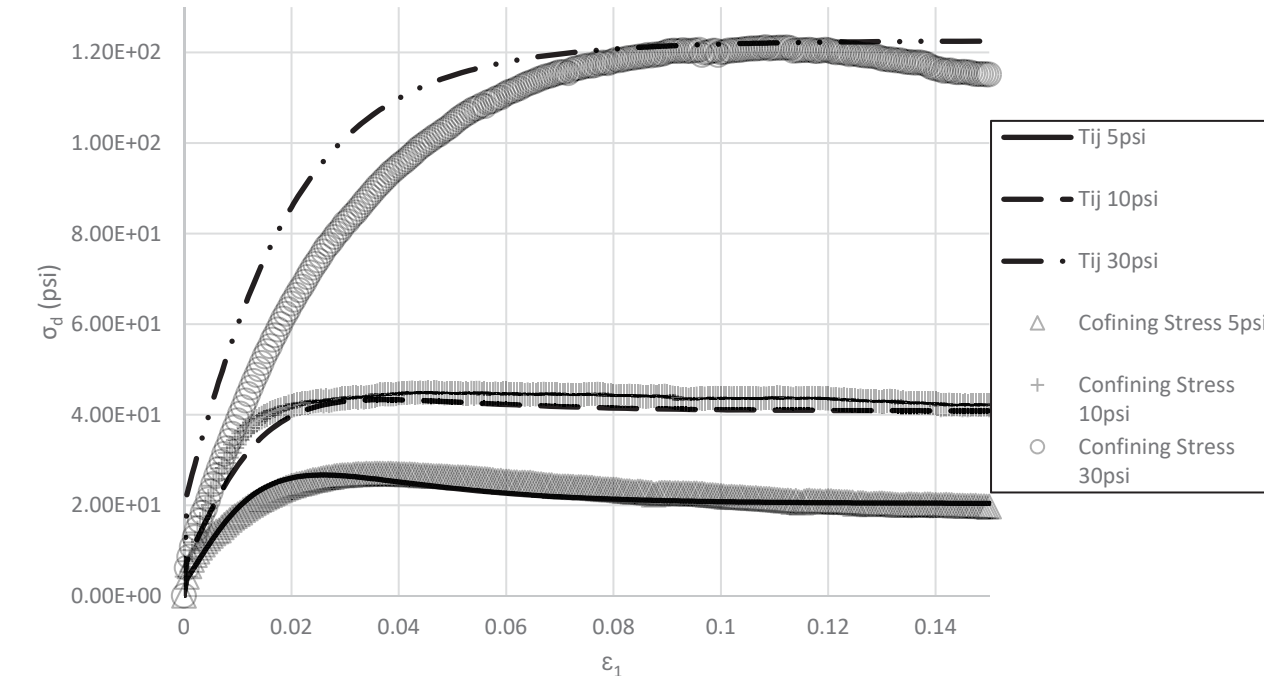
Akaike and Bayesian Info Criteria

R^2

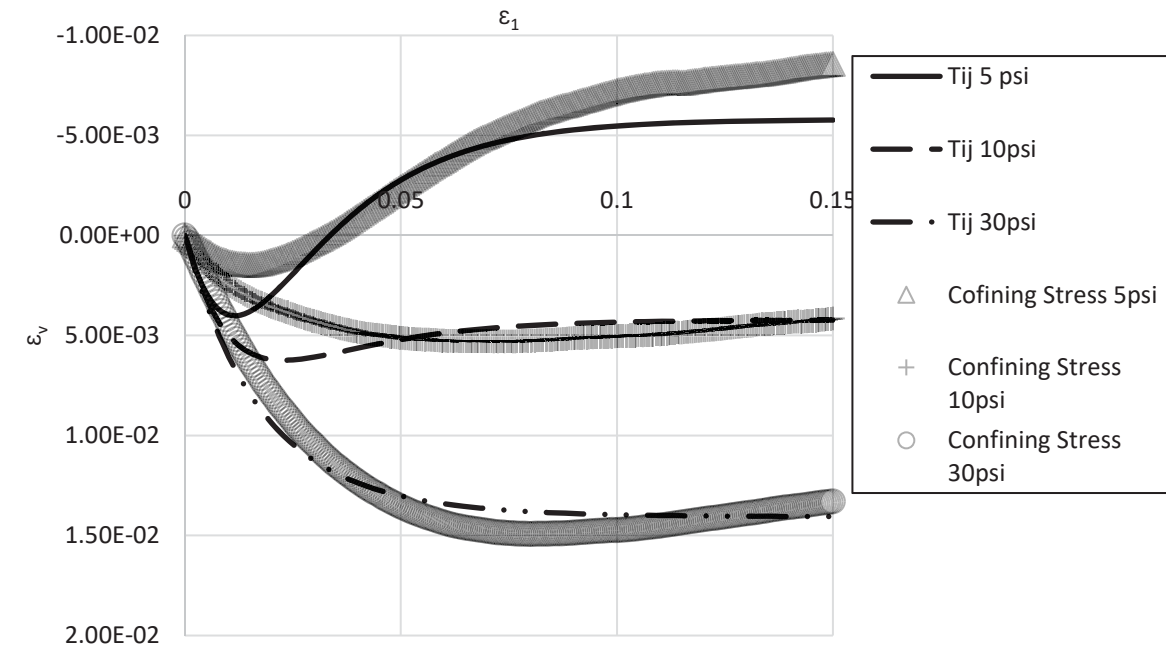
Parameter CI and Standard Error

Parameter Correlation

Deviator Stress vs Axial Strain

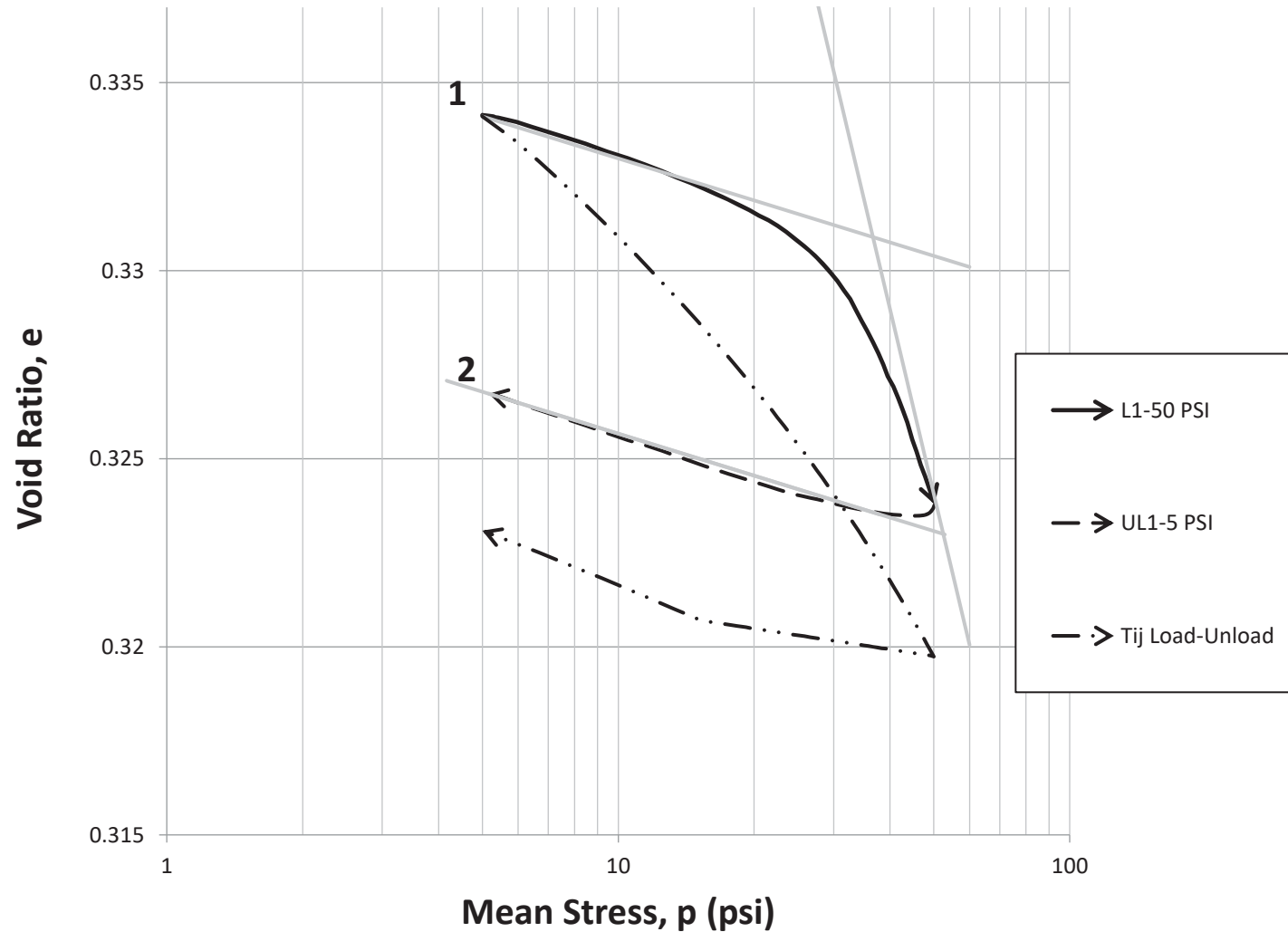


Volumetric Strain vs Axial Strain



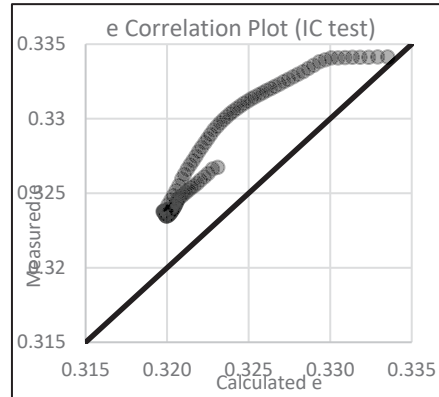
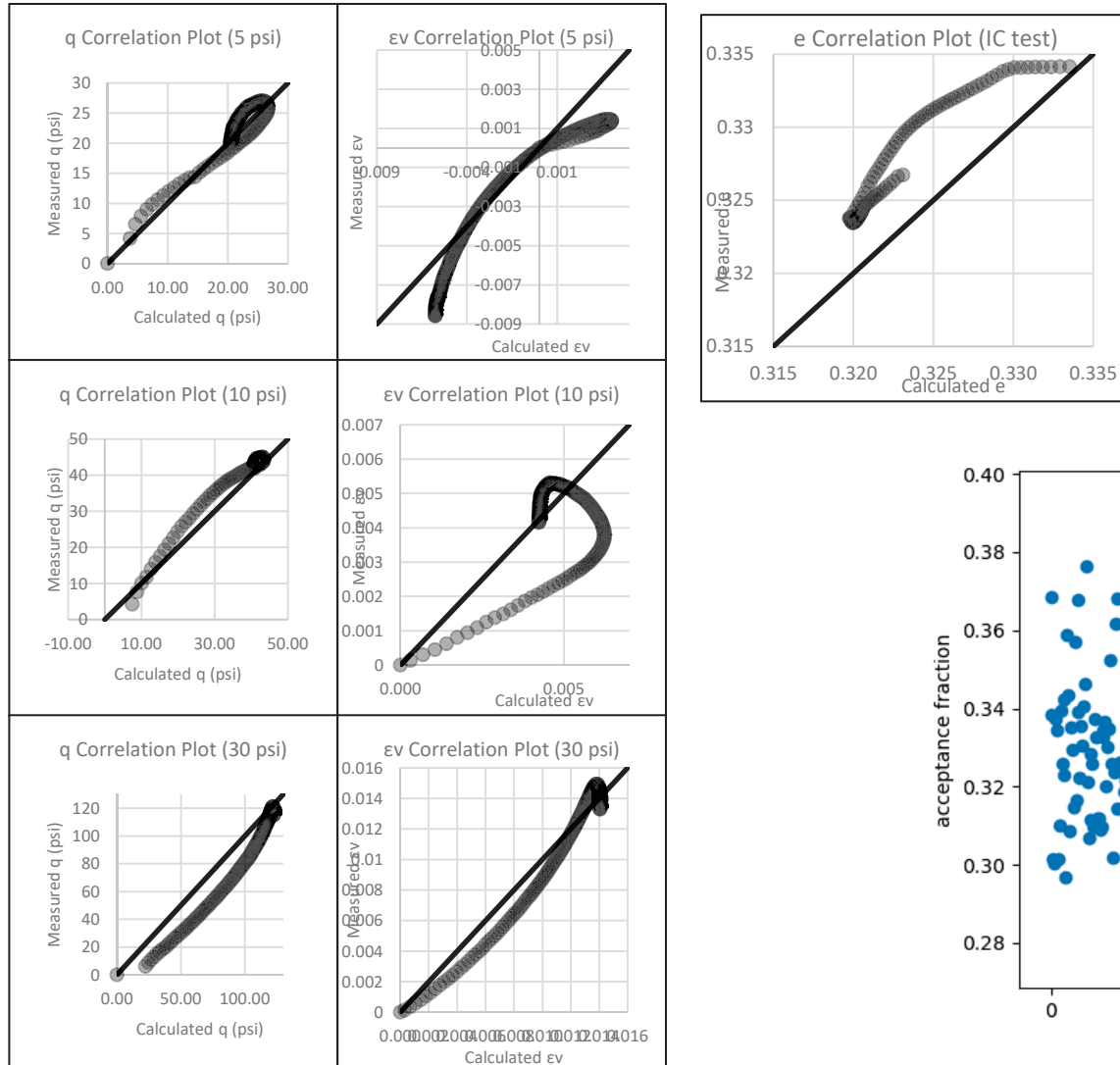
Parameters from Machine Learning but....

機械学習から得られたパラメータだが...

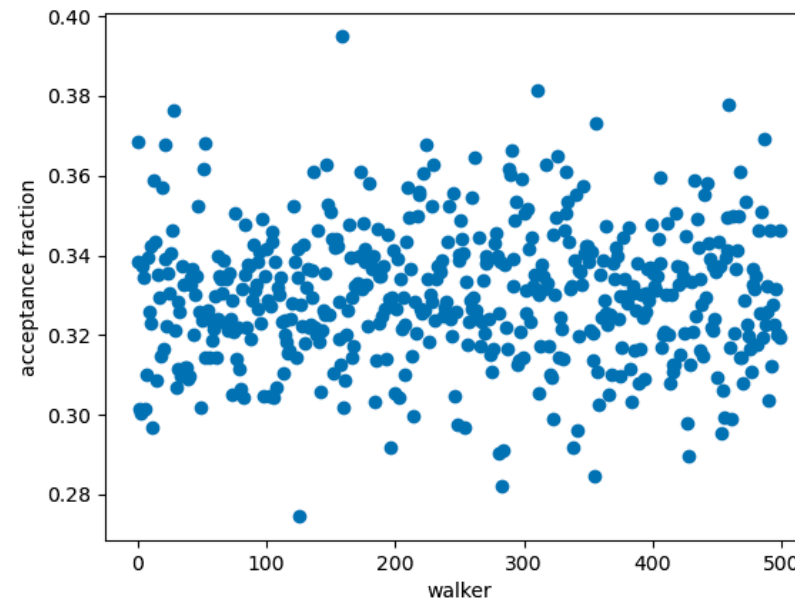


Parameter Results

パラメータの結果

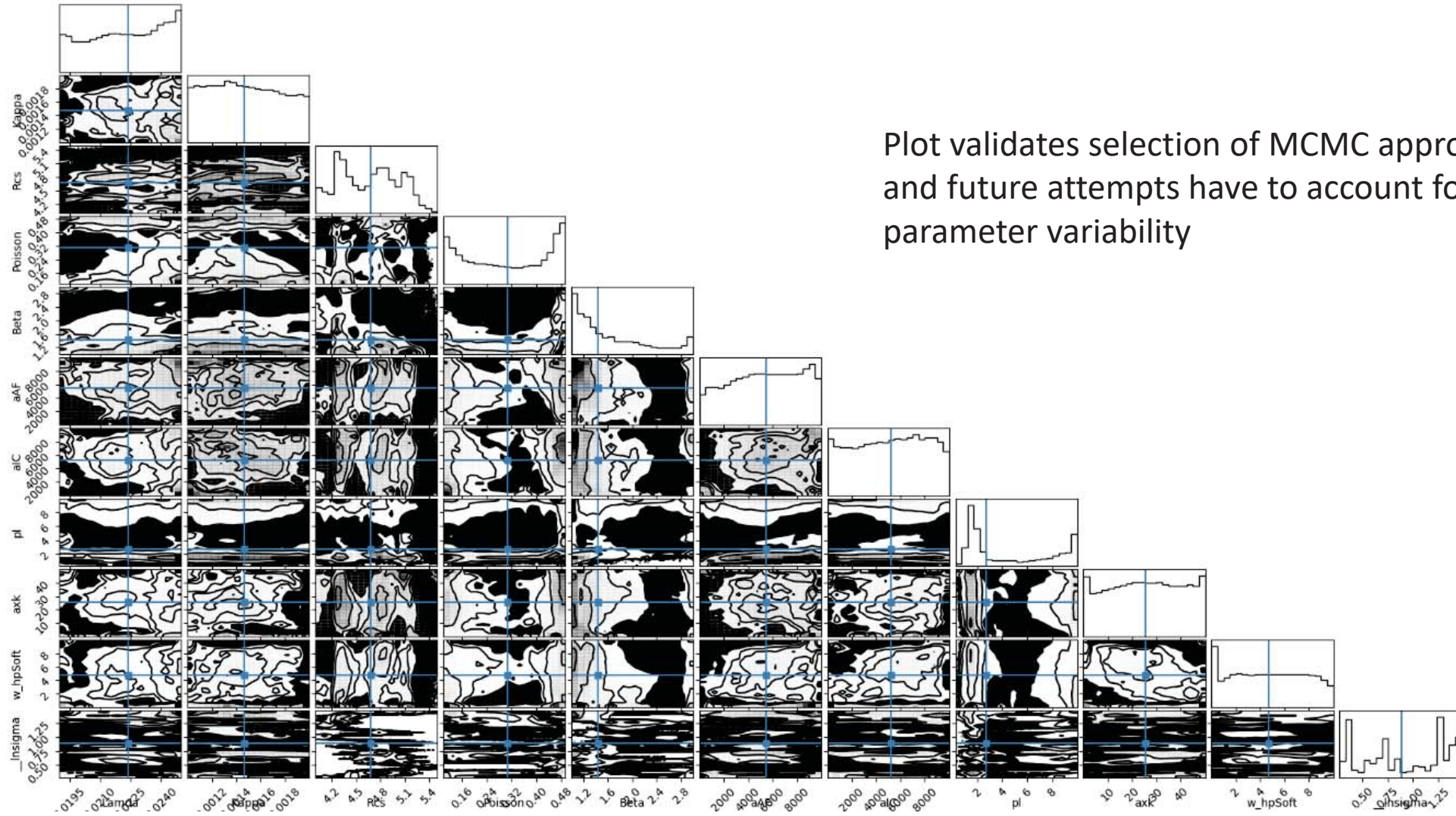


Metric	R ²	R	CoV	SRS	C _v	SRS/CoV
$q (\sigma_3 = 5 \text{ psi})$	0.87149	0.93353	13.2681	776.467	0.16267	58.5215
$q (\sigma_3 = 10 \text{ psi})$	0.97273	0.98627	41.5877	1930.47	0.15394	46.4191
$q (\sigma_3 = 30 \text{ psi})$	0.96990	0.98483	667.609	37600.4	0.25723	56.3210
$\varepsilon_v (\sigma_3 = 5 \text{ psi})$	0.91773	0.95798	1.12E-05	8.19E-04	-0.77546	73.1438
$\varepsilon_v (\sigma_3 = 10 \text{ psi})$	0.11306	0.33625	3.22E-05	67.7767	1.26982	2104572
$\varepsilon_v (\sigma_3 = 30 \text{ psi})$	0.96699	0.98335	1.09E-05	2.26E-04	0.26772	20.6589
e	0.90187	0.94967	1.32E-05	0.10652	0.01109	8082.67
Average	0.82695	0.88519				
Average (w/o ε_v [$\sigma_3 = 10 \text{ psi}$])	0.92894	0.96362				



Parameter Results

パラメータの結果



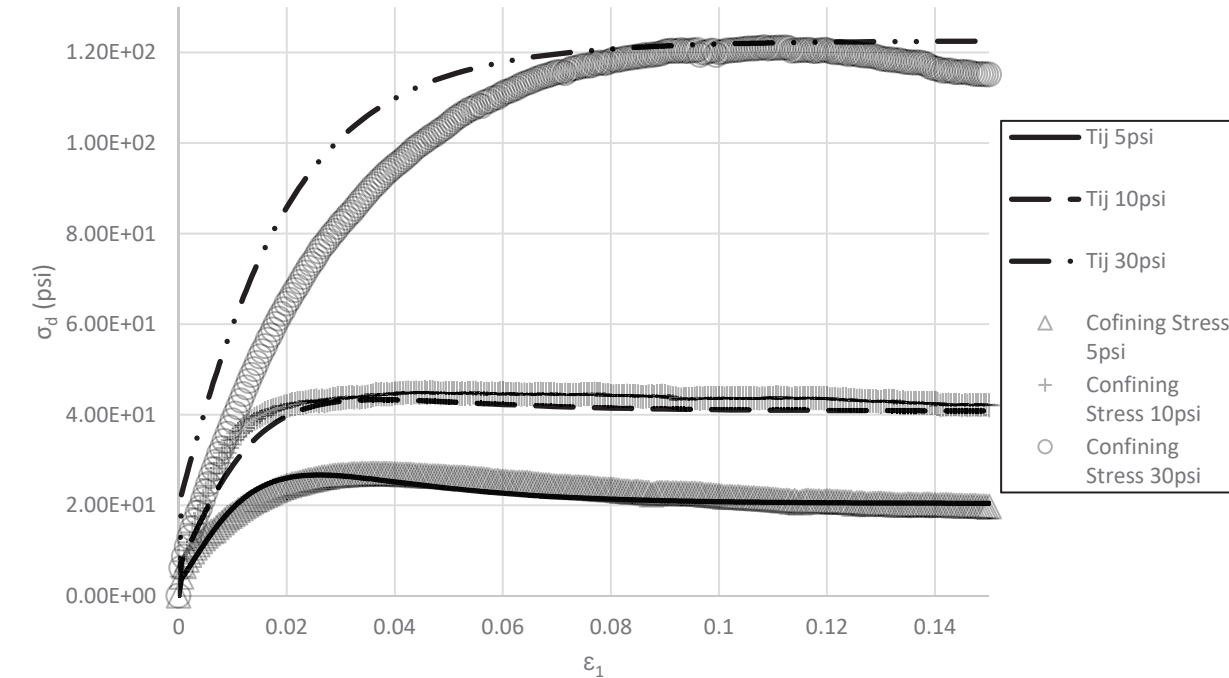
Parameters from Machine Learning

機械学習によるパラメータ

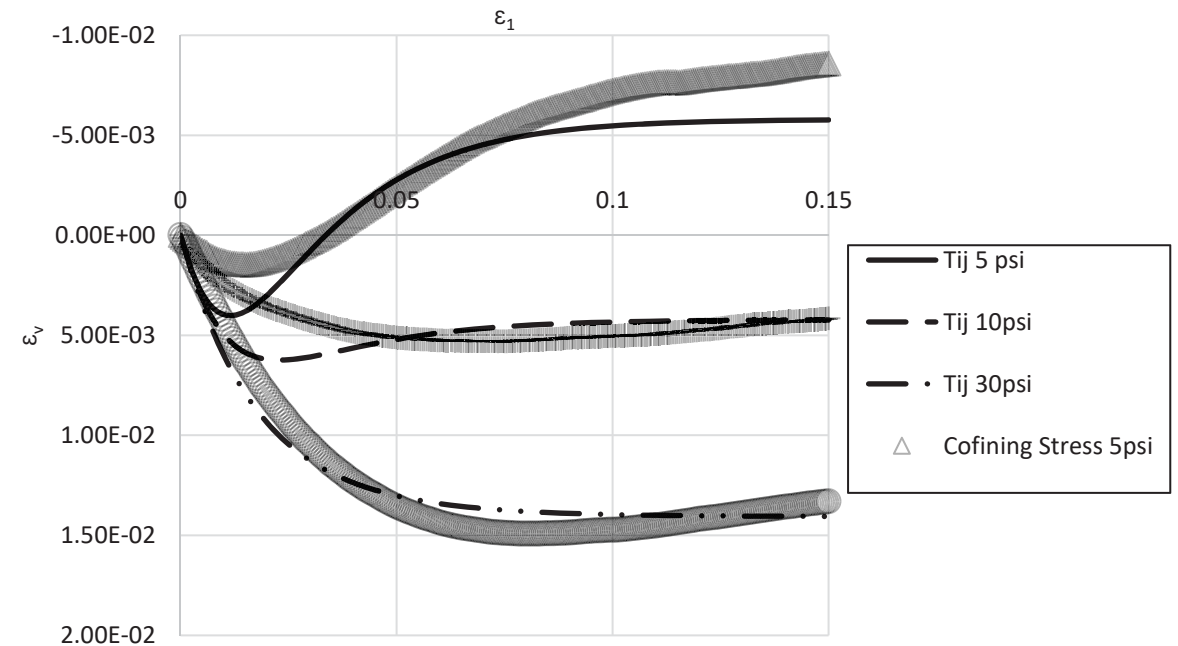


Parameter	Value	Description
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Deviator Stress vs Axial Strain

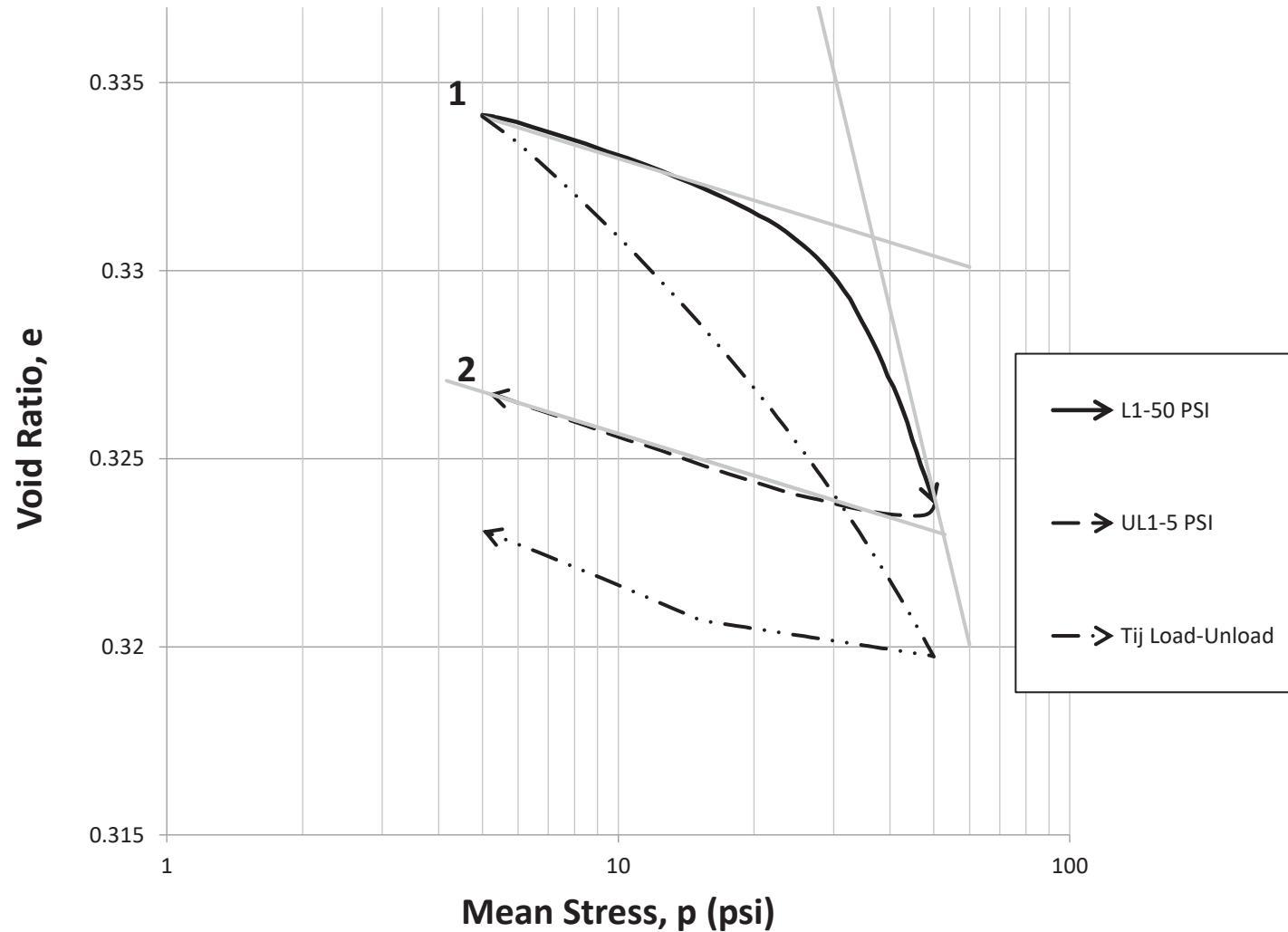


Volumetric Strain vs Axial Strain



Parameters from Machine Learning but....

機械学習から得られたパラメータだが...



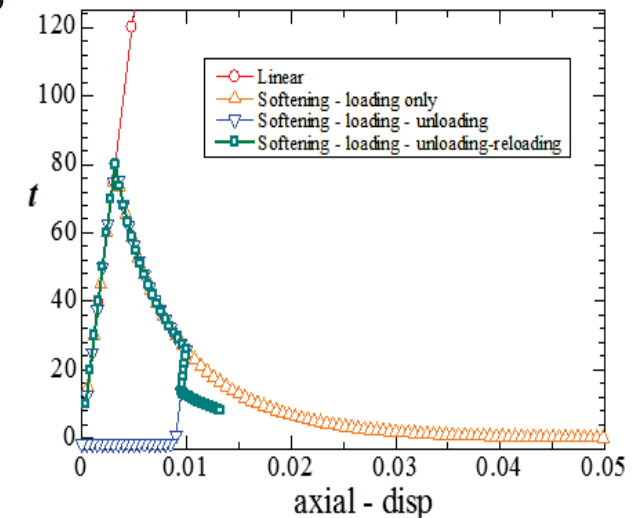
Geotextile Parameters

ジオテキスタイルのパラメータ

Test	Geotextile Manufacturer	Wide Width Tensile Strength (lb/ft)	Wide width tensile strength at 5% strain (lb/ft)	Tensile Strength (Grab) (lb)	Wide Width Elongation (%)
TF-6, -7, TF-9, -10	Propex	4800 x 4800	660 x 1500	600 x 500	(10 x 8%)

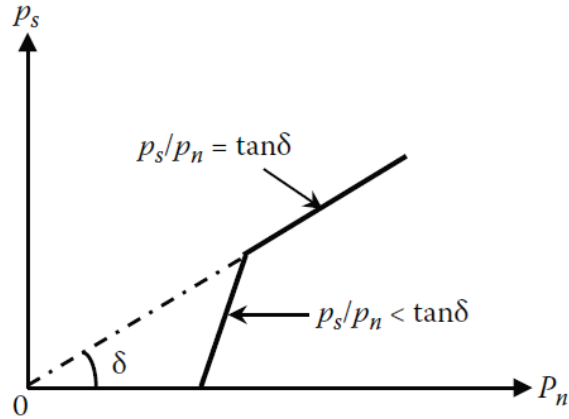
- Biaxial, woven polypropylene Propex Geotex 4X4HF geotextile
- Ideally want geotextile strength to decay after yield
- Geotextile modeled as biaxial, bilinear elastoplastic

Geotextiles		
Parameter	Value	Unit
EA_1	876	kN/m
EA_2	701	kN/m
T_f	70.05	kN/m

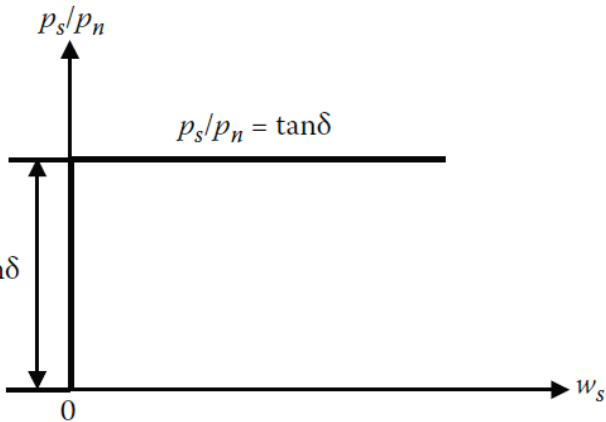


Geotextile wide width tensile force vs axial strain

Interface Elements インターフェース要素



(a) Relation between normal stress (p_n) and shear stress (p_s)



(b) Relation between relative displacement (w_s) and stress ratio (p_s/p_n)

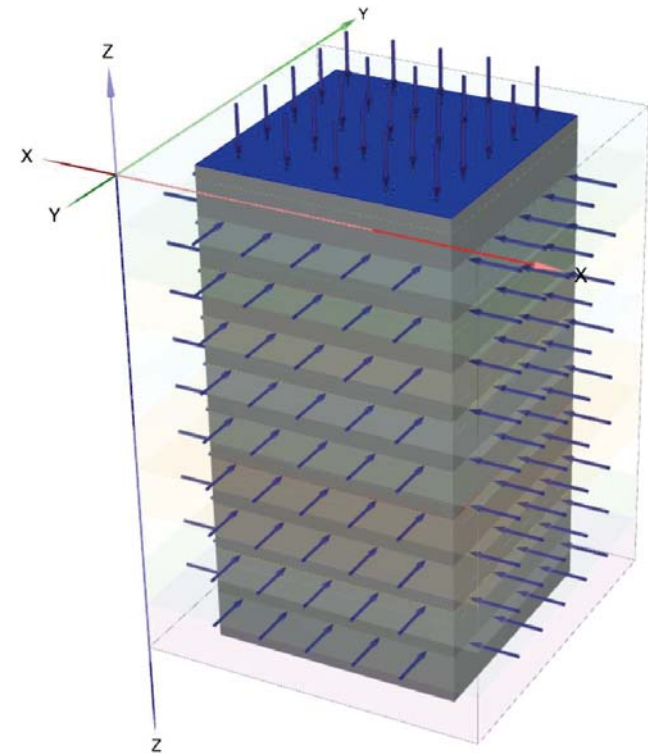
Idealized interface behavior (Nakai T., 2013)
Idealized interface behavior (Nakai T., 2013)

Interface (Geotextile-Soil)		
Parameter	Value	Unit
k_n	$100.0 * 10^6$	kN/m ³
k_s	$9.09 * 10^6$	kN/m ³
ν	0	-
ϕ	40	°
ψ	0	°
C_{ref}	0	kPa
Interface (Footing-Soil)		
Parameter	Value	Unit
k_n	$100.0 * 10^6$	kN/m ³
k_s	$9.09 * 10^6$	kN/m ³
ν	0	-
ϕ	44	°
ψ	0	°
C_{ref}	0	kPa

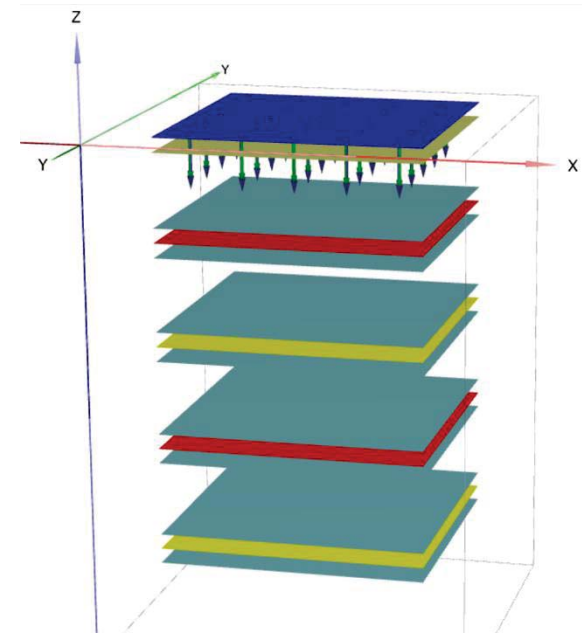
Geo-Research Institute (2022)

Modelling of TF10 and TF7

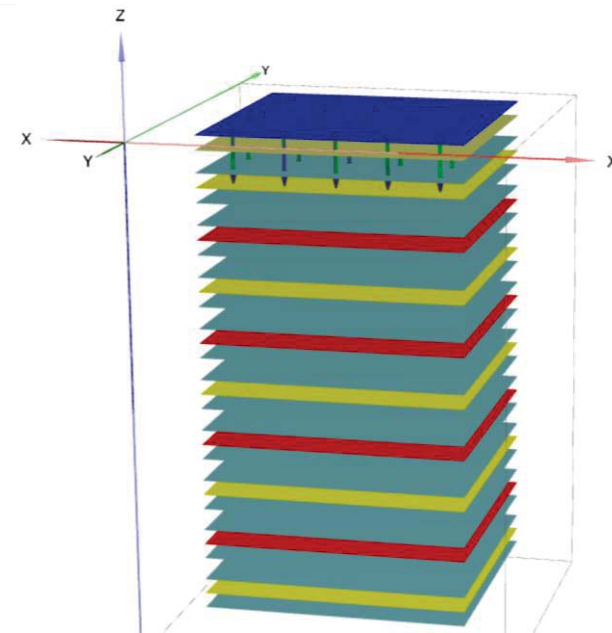
TF10およびTF7のモデル化



PLAXIS®



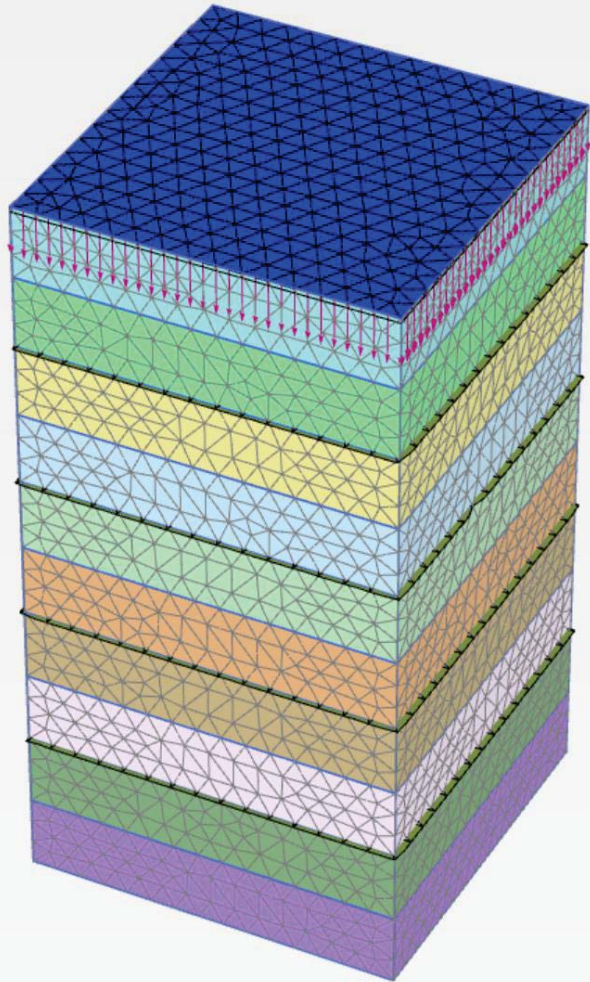
TF10



TF7

Modelling of TF10

TF10のモデル化



Name	Value
General	
ID	Phase_1
Start from phase	Initial phase
Calculation type	Plastic
Loading type	Staged construction
ΣM_{stage}	1.000
ΣM_{weight}	1.000
Pore pressure calculation type	Phreatic
Time interval	0.000 day
First step	1
Last step	100
Special option	0
Deformation control parameters	
Ignore undr. behaviour (A,B)	☐
Reset displacements to zero	☒
Reset small strain	☒
Reset state variables	☐
Reset time	☐
Updated mesh	☐
Ignore suction	☒
Cavitation cut-off	☐
Cavitation stress	100.0 kN/m ²
Numerical control parameters	
Solver type	Pardiso (multicore direct)
Max cores to use	256
Max number of steps stored	1
Use compression for result files	☐
Use default iter parameters	☐
Max steps	1000
Tolerated error	0.5000
Max unloading steps	5
Max load fraction per step	0.01000
Over-relaxation factor	1.200
Max number of iterations	60
Desired min number of iterations	6
Desired max number of iterations	15
Arc-length control type	Auto
Use subspace accelerator	☐
Subspace size	3
Use line search	☒
Use gradual error reduction	☐

Soil - User-defined - GW1

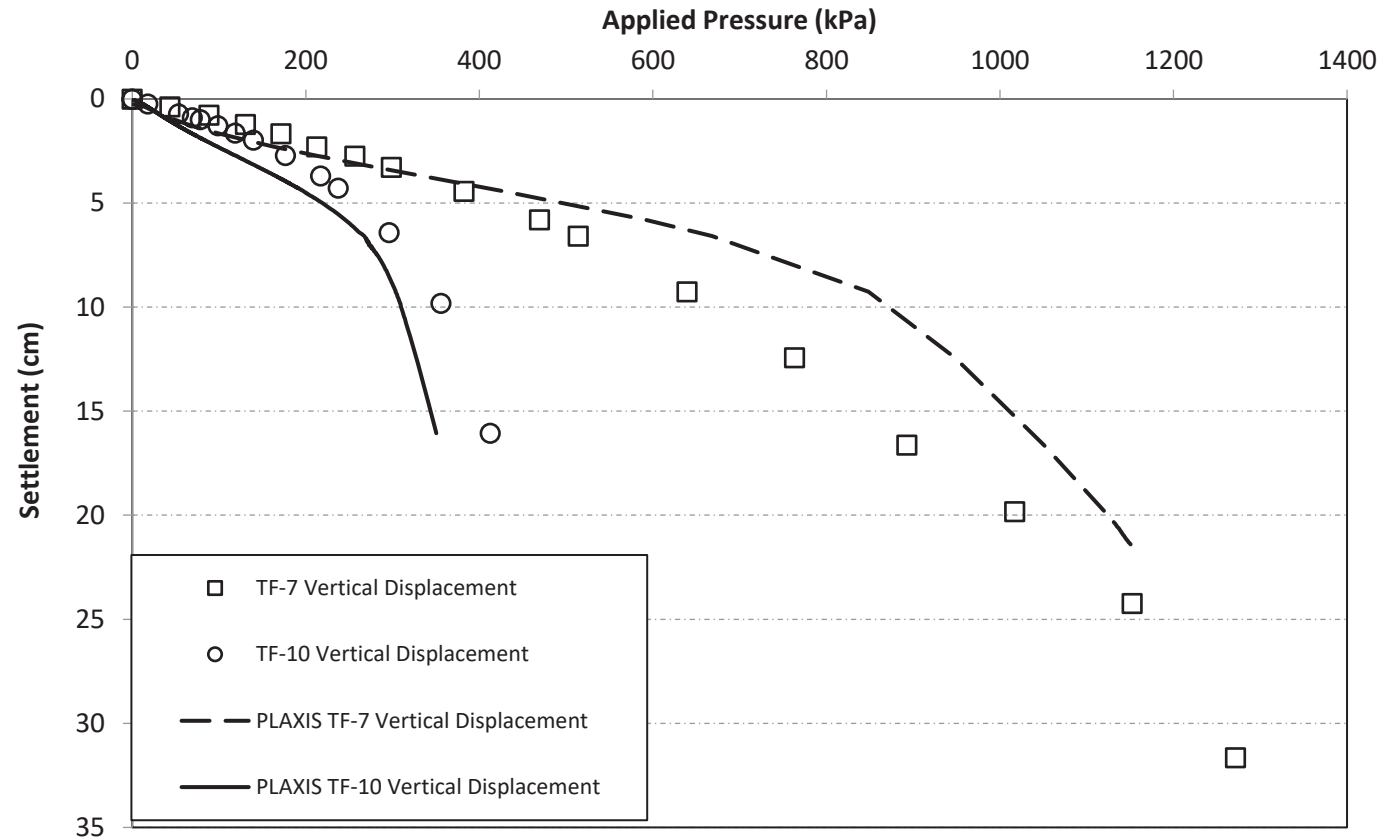
General Mechanical Groundwater Interfaces Initial

Property	Unit	Value
User-defined model		
DLL file		tj120plaxis_3dexp6-4.dll
Model in DLL		NoTension/Subloading tj AF
User-defined parameters		
λ		0.03250
κ		1.600E-3
R_{cs}		5.000
N (void ratio under atmospheric pressure)		0.3640
ν (Poisson ratio)		0.2000
Beta (Shape of yield surf. Beta > 1.0 is recommended)		1.155
e_0 (void ratio under initial stress)		0.2450
[Density] a		400.0
[Density] k_s		10.00
[Bonding] Q_{c0}		0.000
[Bonding] b		0.000
[Bonding] k_b		0.000
[Unit] Pa (Atmospheric pressure) [Be careful of what unit system you use]	kN/m ²	100.0
[IC component] wgtIC		1.000
[IC component] powerIC		2.000
[Advanced] SplitStrainFlag (You should let it be 0.0.)		0.000
[Advanced][e_0] e_{0inc}		0.000
[Advanced][e_0] z_{ref}	m	0.000
[Advanced][e_{max}] e_{max}		0.5510

Next OK Cancel

Load-settlement

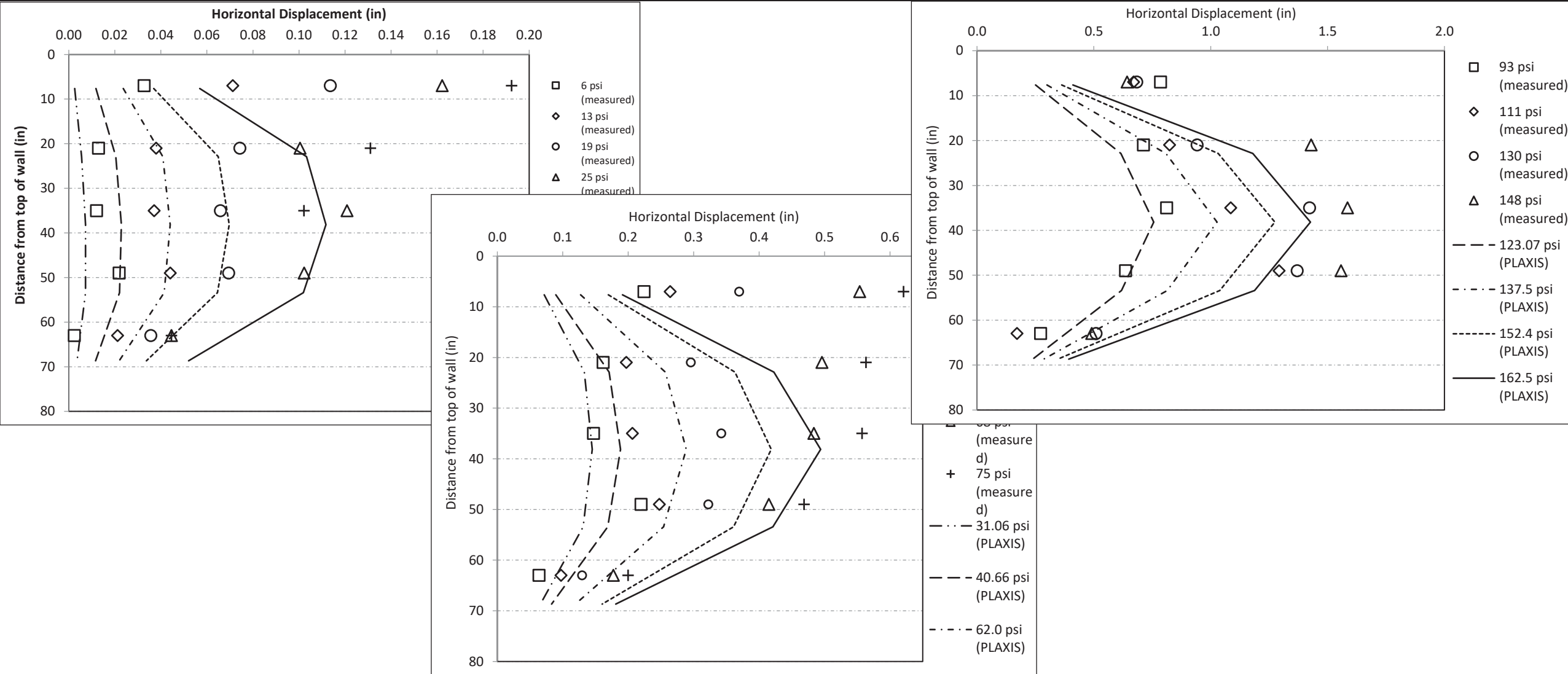
荷重-沈下関係



GRS Pier	R ²	R	CoV	SRS	C _v	SRS/CoV
TF - 7	0.96413	0.98190	150905	1.73E+05	0.883934	1.145405
TF - 10	0.99046	0.99522	16753	3.72E+04	0.720752	2.22
Average	0.97730	0.98856				

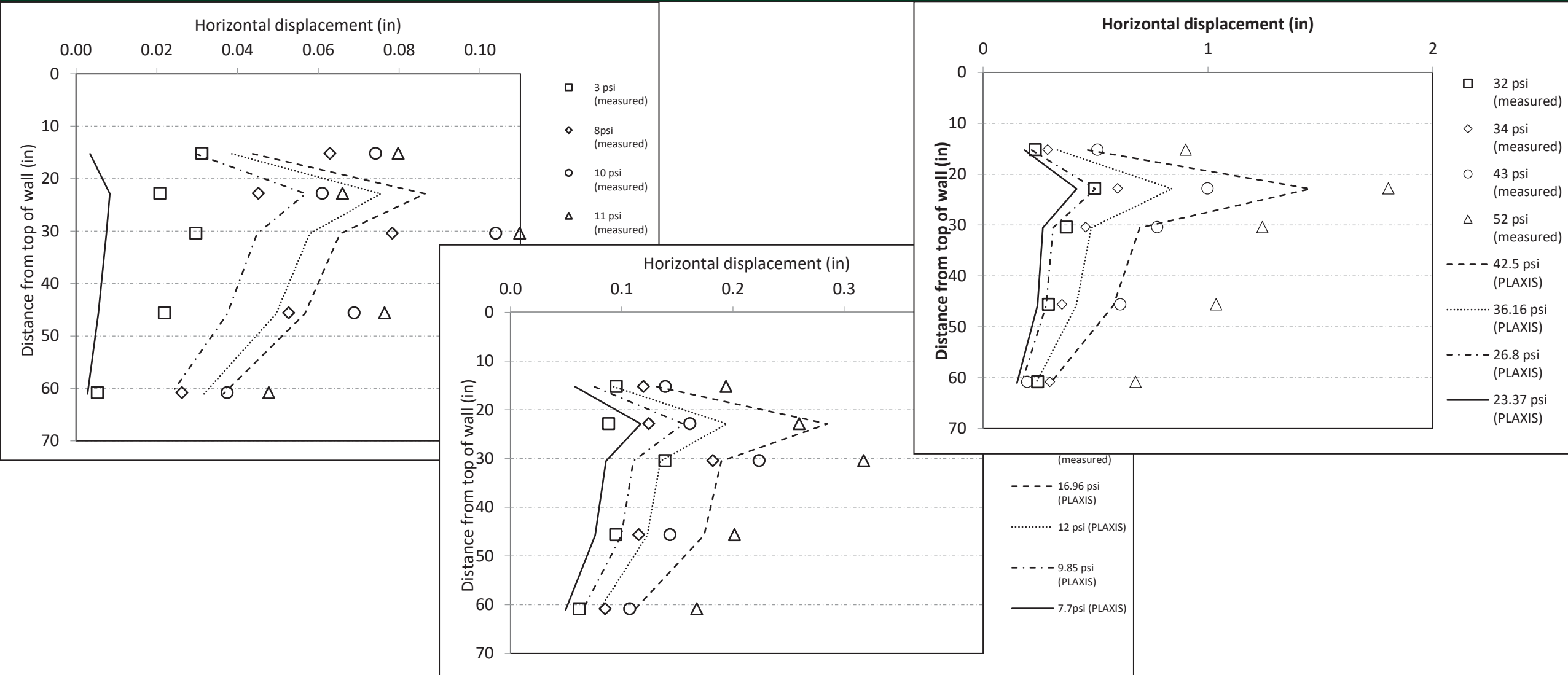
Lateral Deformation TF7

TF7の水平変形



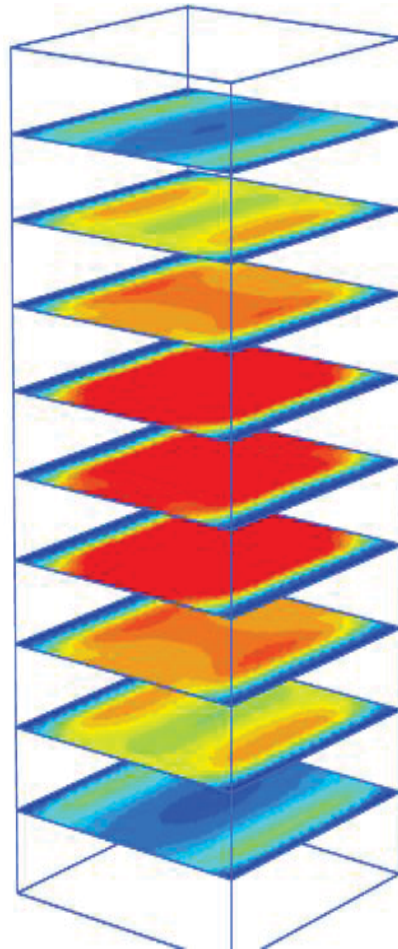
Lateral Deformation TF10

TF10の水平変形

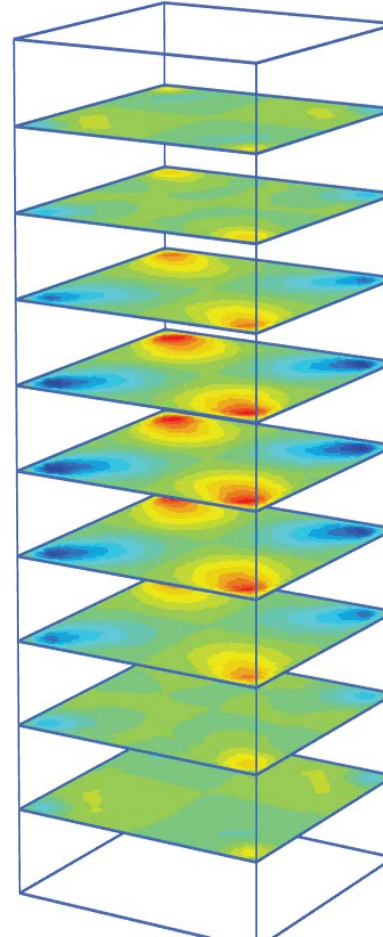
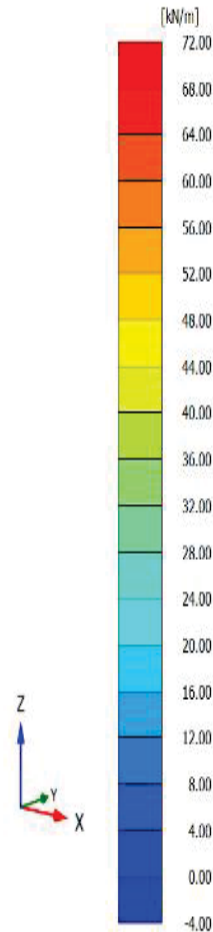


Geotextile Force Distribution in TF7

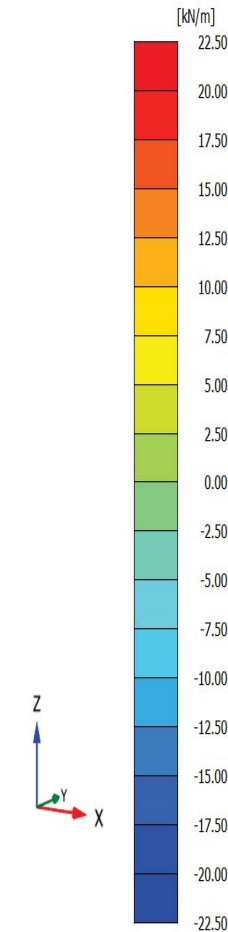
TF7におけるジオテキスタイルの張力分布



N_1 (in-plane force, kN/m)

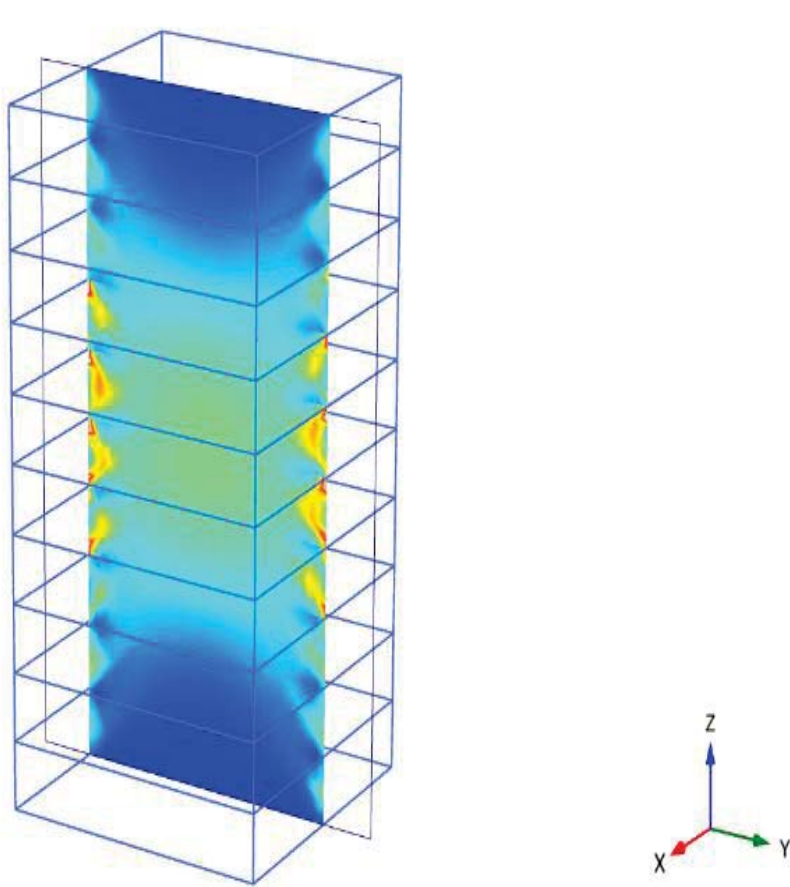


Q_{12} (in-plane shear, kN/m) - Right

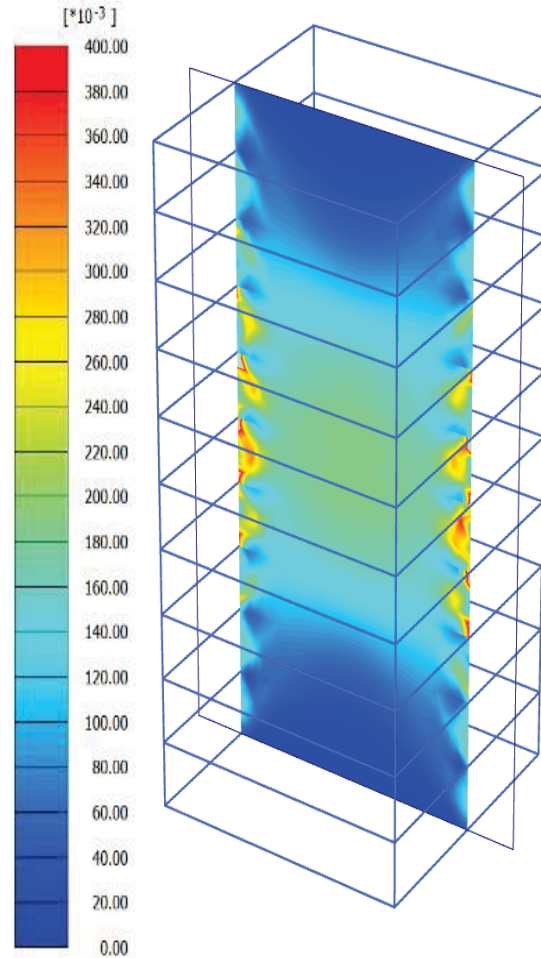


Deviatoric Strain, γ_s , Distribution in TF7

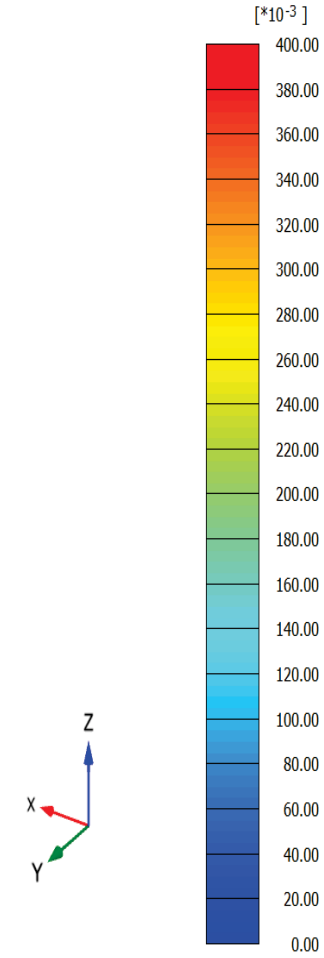
TF7の偏差ひずみ (γ_s) の分布



YZ cross-section

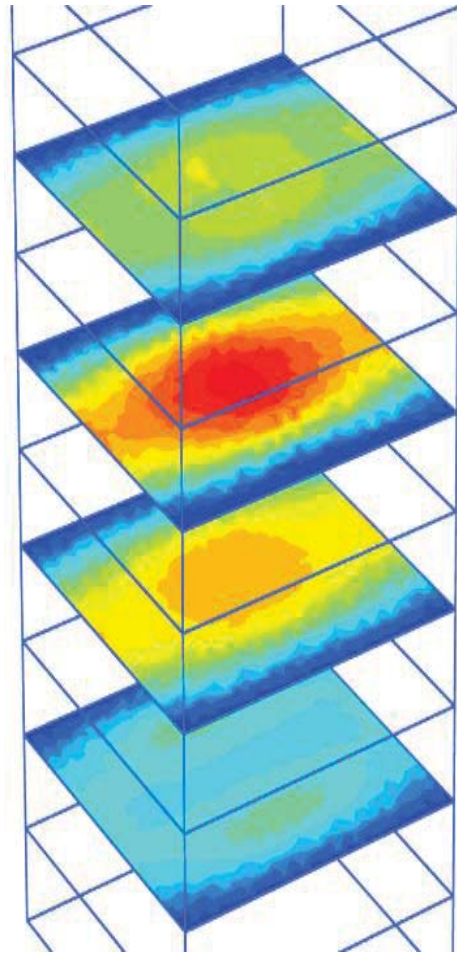


XZ cross-section

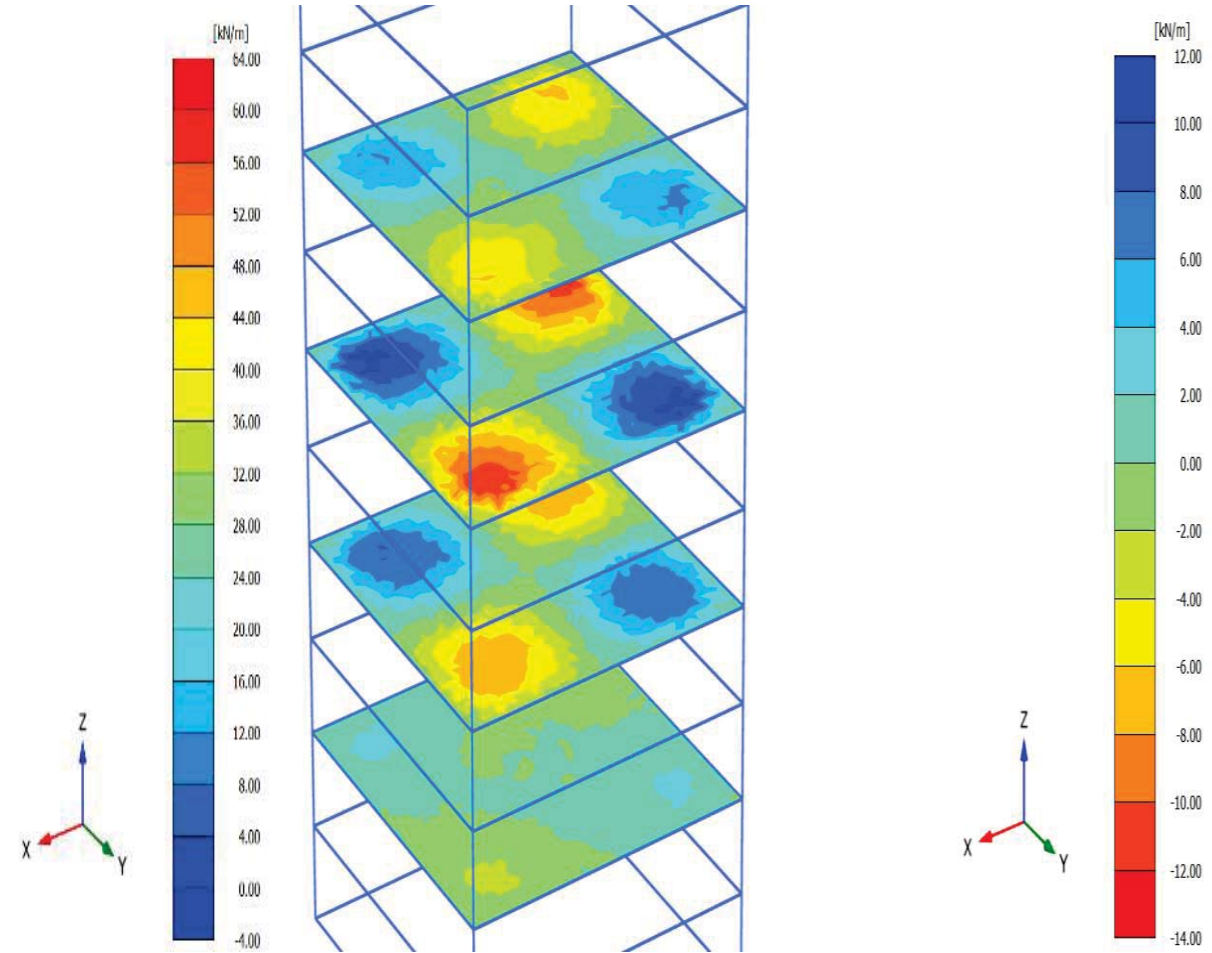


Geotextile Force Distribution in TF10

TF10におけるジオテキスタイルの張力分布



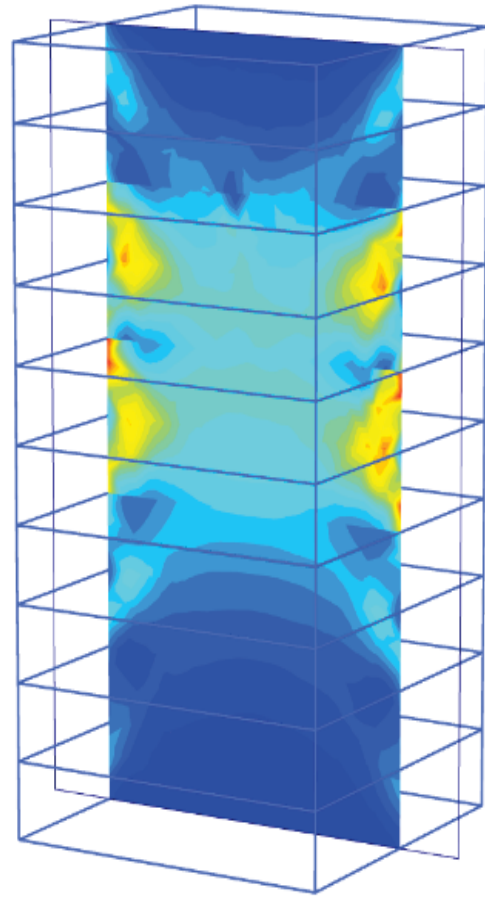
N_1 (in-plane force, kN/m)



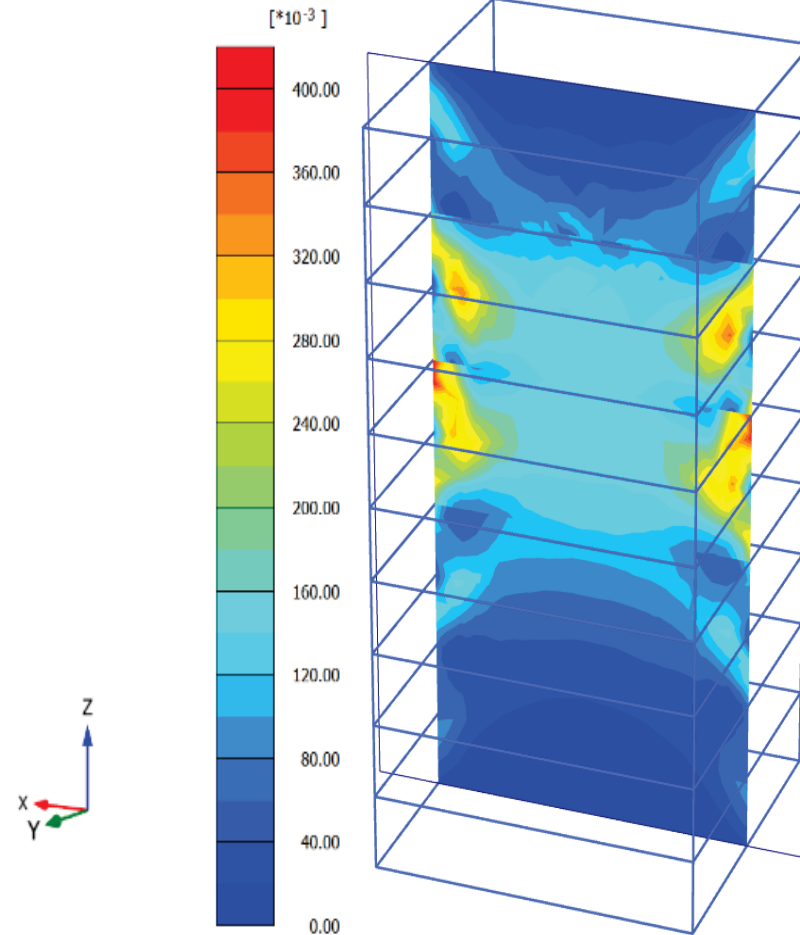
Q_{12} (in-plane shear, kN/m) - Right

Deviatoric Strain, γ_s , Distribution in TF10

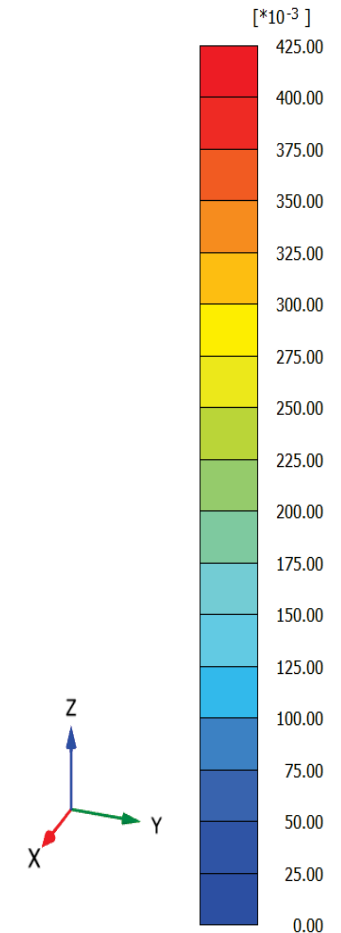
TF10の偏差ひずみ (γ_s) の分布



XZ cross-section



YZ cross-section



Summary and Conclusions

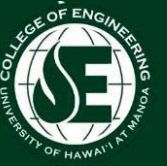
まとめと結論



- Using machine learning, optimization of parameters should be performed for both triaxial compression and consolidation tests with appropriate weighting for each
- Combined FEM with DEM may be necessary to consider spalling of soil in unfaced GRS columns
- Beginnings of shear planes can be seen in deviatoric strain plots despite use of associated plasticity in Subloading t_{ij} model
- Stress development primarily occurred in the central geotextile reinforcement layers

Summary and Conclusions

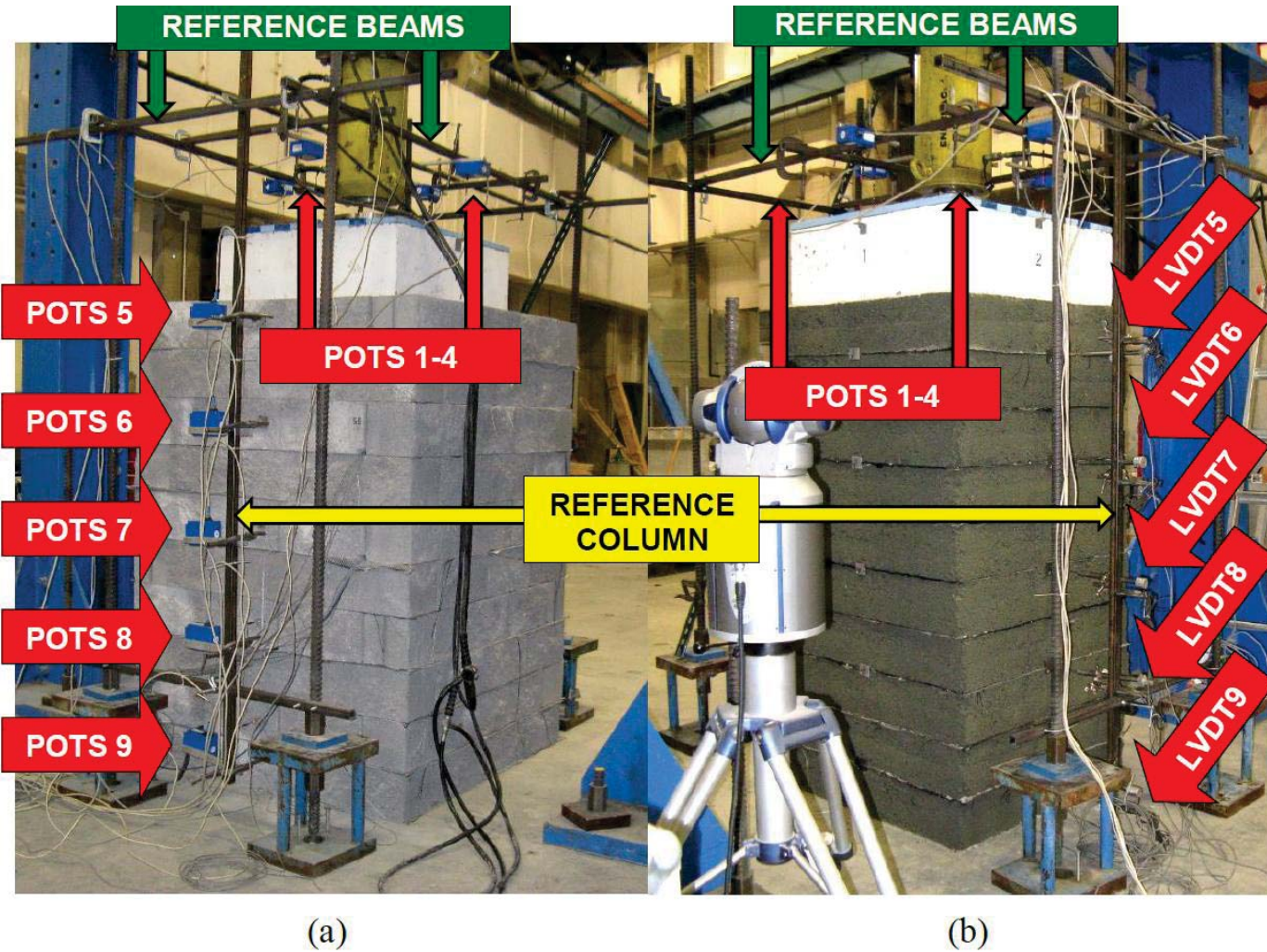
まとめと結論



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Load Testing

載荷試驗



Schematics of deflection instrumentation for mini piers (a) with facing and (b) without facing. (Iwamoto, 2014)



TF-10 at failure with $S_v = 15\frac{1}{4}$ inches, $T_f = 4,800$ lb/ft, and VDOT 21A material. (Nicks et al., 2013)

Summary and Conclusions

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Thank You

